# Analysis of isothermal EOS for NaCl under extreme compression 

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## Introduction

The exploration of matter at extreme conditions is a central theme in a broad range of scientific disciplines (e.g. material science, chemistry, physics and Earth and planetary science). The application of pressure can induces both continuous and discontinuous changes in atomic and electronic structure of a material. Learning how atomic and electronic arrangements change under extreme conditions, provide insight into the nature of phase transformations, chemical reaction, and also evolution in micro- and nanostructural components, such as crystallite size, dislocations, voids, and grain boundaries. Once these processes are understood, it will be possible to predict responses of materials under thermo-mechanical extremes using advanced computational tools. Further, this fundamental knowledge will open new avenues for designing and synthesizing materials with unique properties. These thermo-mechanical extremes will allow the tuning of atomic structure and the varying nature of chemical bonds to produce revolutionary new materials.

The properties of solids at high pressure and temperature are very important for their application point of view. NaCl is an important alkali halide that is used as a pressure gauge in laboratory measurements of compression data. It is one of the most widely used internal pressure standards in high-pressure diffraction experiments owing to the availability of a large body of experimental data. For instance, the equation of state for B1type NaCl has been investigated in several studies up to the limit of its stability [1-8]. It is also known that the $B 1$-type NaCl is only stable up to a pressure of about 30 GPa , where the occurrence of a pressure-induced phase transition from $B 1$ type (rocksalt) to B2-type (cesium chloride) as it has been reported by different group of researchers. [9-15] Although it is experimentally possible to study the $B 2$-type NaCl at elevated pressures, its equation of state has not been investigated well yet, especially at high temperatures. This, therefore, limits the use of NaCl as a pressure standard to relatively low pressures and temperatures. Therefore, the $P-V-T$ equation of state


#### Abstract

Different isothermal EOS, which expresses volume ratio as a function of pressure for materials at given temperature has been discussed. During our computational investigation it is observed that Holzapfel EOS does not satisfy the agreement of $K_{T} K_{T}^{\prime \prime}$ as calculated by using Brennan Stacey EOS, Shanker EOS, and Vinet EOS. The critical test of EOS for solids under extreme compressions has been discussed by evaluating the pressure and volume derivative properties viz. isothermal bulk modulus and its pressure derivative, according to the data calculated for NaCl up to extremely high pressure. Among the four EOS viz Holzapfel EOS, Brennan Stacey EOS, Shanker EOS, and Vinet EOS, it is found that, Holzapfel EOS is not suitable for calculating higher pressure derivative of isothermal bulk modulus under extreme compression


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The Shanker EOS derived using a modified exponential dependence for the short range constant on volume [20] is as follows:
$P=\frac{3 K_{0}\left(\frac{V}{V_{0}}\right)^{-\frac{4}{3}}}{\left(3 K_{0}^{\prime}-8\right)}\left[\left(1-\frac{1}{t}+\frac{1}{t^{2}}\right)(\exp t y-1)+y\left(1+y-\frac{2}{t}\right) \exp t y\right]$

Where $y=\left(1-\frac{V}{V_{0}}\right)$ and $t=\left(K_{0}^{\prime}-\frac{8}{3}\right)$
Vinet EOS based on universal relationship between binding energy and interatomic separation for solids $[21,22]$ is as follows:

$$
\begin{equation*}
P=3 K_{0} x^{-2}(1-x) \exp [\eta(1-x)] \tag{4}
\end{equation*}
$$

Where $\quad \eta=\frac{3}{2}\left(K_{0}^{\prime}-1\right)$
Expression for isothermal bulk modulus corresponding to equations (1), (2) and (3) obtained by using the relationship $K_{T}=-V\left(\frac{d P}{d V}\right)_{T}$ given as
$K_{T}=\frac{1}{3} f P x-K_{0} x^{-5}(4 x-5) \exp [f(1-x)]$
$K_{T}=K_{0}\left(\frac{V}{V_{0}}\right)^{-\frac{1}{3}} \exp \left\{\left(K_{0}^{\prime}-\frac{5}{3}\right)\left(1-\frac{V}{V_{0}}\right)\right\}+\frac{4}{3} P$
$K_{T}=\frac{4}{3} P+K_{0}\left(\frac{V}{V_{0}}\right)^{-\frac{4}{3}} \exp \left\{\left(K_{0}^{\prime}-\frac{8}{3}\right)\left(1-\frac{V}{V_{0}}\right)\right\}$
and
$K_{T}=K_{0} x^{-2}[1+(\eta x+1)(1-x)] \exp \{\eta(1-x)\}$
The expression for first pressure derivative of isothermal bulk modulus can be given as
$K_{T}^{\prime}=\frac{\partial K_{T}}{\partial P}=\frac{\partial K_{T}}{\partial V} \frac{\partial V}{\partial P}$
Using expression (9) in equations (5), (6), (7) and (8), the first derivative of isothermal bulk modulus $K_{T}^{\prime}$ becomes
$K_{T}^{\prime}=\frac{f x}{3}\left[\left(1-\frac{P}{3 K_{T}}\right)-\frac{1}{K_{T}}\left(\frac{f P x}{3}-K_{T}\right)\right]-\frac{K_{0} x^{-5}}{3 K_{T}}(16 x-25) \exp [f(1-x)]$
$K_{T}^{\prime}=\frac{16}{9} \frac{P}{K_{T}}+\left(1-\frac{4 P}{3 K_{T}}\right)\left\{\frac{V}{V_{0}}\left(K_{0}^{\prime}-\frac{5}{3}\right)+\frac{5}{3}\right\}$
$K_{T}^{\prime}=\frac{16}{9} \frac{P}{K_{T}}+\left(1-\frac{4 P}{3 K_{T}}\right)\left\{\frac{V}{V_{0}}\left(K_{0}^{\prime}-\frac{8}{3}\right)+\frac{8}{3}\right\}$
and

$$
\begin{equation*}
K_{T}^{\prime}=\frac{1}{3}\left[\frac{x(1-\eta)+2 \eta x^{2}}{1+(\eta x+1)(1-x)}+\eta x+2\right] \tag{12}
\end{equation*}
$$

The corresponding expression for second order pressure derivative of isothermal bulk modulus
$K_{T}^{\prime \prime}=\frac{\partial K_{T}^{\prime}}{\partial P}$, obtained from further derivation of (10), (11), (12) and (13) are written as follows:

$$
\begin{align*}
K_{T} K_{T}^{\prime \prime}= & -\frac{f x}{9}\left[2\left(1-\frac{f P x}{3 K_{T}}\right)-\frac{P}{3 K_{T}}+\left(1-\frac{P K_{T}^{\prime}}{K_{T}}\right)(1+f x)\right]+\frac{K_{0}}{3 K_{T}} \times \\
& {\left[\left\{\left(16 x^{-4}-25 x^{-5}\right)\left(K_{T}^{\prime}-\frac{f x}{3}\right)\right\}-\frac{1}{3}\left\{64 x^{-4}-125 x^{-5}\right\}\right] \exp [f(1-x)] } \tag{14}
\end{align*}
$$

$K_{T} K_{T}^{\prime \prime}=\frac{16}{9}-\frac{16 K_{T}^{\prime}}{9 K_{T}}-\frac{V}{V_{0}}\left(K_{0}^{\prime}-\frac{5}{3}\right)\left(1-\frac{4 P}{3 K_{T}}\right)-\frac{4}{3}\left(1-\frac{P K_{T}^{\prime}}{K_{T}}\right)\left\{\frac{V}{V_{0}}\left(K_{0}^{\prime}-\frac{5}{3}\right)+\frac{5}{3}\right\}$
$K_{T} K_{T}^{\prime \prime}=\frac{4}{3}\left[1-\frac{P K_{T}^{\prime}}{K_{T}}\right]\left[\frac{4}{3}-\left\{\frac{V}{V_{0}}\left(K_{0}^{\prime}-\frac{8}{3}\right)+\frac{8}{3}\right\}\right]-\frac{V}{V_{0}}\left(K_{0}^{\prime}-\frac{8}{3}\right)\left(1-\frac{4 P}{3 K_{T}}\right)$
and

$$
\begin{equation*}
K_{T} K_{T}^{\prime \prime}=\frac{x}{9}\left[\frac{\left\{x(1-\eta)+2 \eta x^{2}\right\}\{\eta(1-2 x)-1\}}{\{1+(\eta x+1)(1-x)\}^{2}}-1-4 \eta x\right] \tag{16}
\end{equation*}
$$

## Results and Discussion

In the present work we have described four different forms of EOS, equtions (1), (5), (10) and (14) corresponds for Holzapfel EOS, equation (2), (6), (11) and (15) corresponds for Brennan Stacey EOS, equations (3), (7), (12) and (16) corresponds for Shanker EOS and equations (4), (8), (13) and (17) corresponds for Vinet EOS. All the four EOS contains only two parameters $K_{0}$ and $K_{0}^{\prime}$ both at zero pressure at different temperature. These values of $K_{0}$ and $K_{0}^{\prime}$ have been recommended by Anderson [23]. The value of input parameters $K_{0}(\mathrm{GPa})$ and $K_{0}^{\prime}$ given in the Table-1 are obtained from the literature [24-26]. The values of pressure $\mathrm{P}(\mathrm{GPa})$ for NaCl were computed for given increments of $V / V_{0}$ by using equation (1), (2), (3)and (4) at different temperature ranges from 300K-1050K.
Using the value of pressure P computed as above, the value of isothermal bulk modulus $K_{T}$ has been calculated by using equation (5), (6), (7) and (8). Substituting these values of P and $K_{T}$ in equation (10), (11), (12) and (13), the values of first pressure derivative of $K_{T}$ i.e. $K_{T}^{\prime}$ have been obtained. Further substituting the values of $\mathrm{P}, K_{T}, K_{T}^{\prime}$ in equation (14), (15), (16)
and (17), second pressure derivative of $K_{T}$ i.e. $K_{T}^{\prime \prime}$ has been calculated in terms of $K_{T} K_{T}^{\prime \prime}$.
These calculated values of $\mathrm{P}, K_{T}, K_{T}^{\prime}$ and $K_{T} K_{T}^{\prime \prime}$ for NaCl at different temperature shown in Table (2-7). The graphs plotted between $V / V_{0} \quad$ vs $\mathrm{P}, \mathrm{P}$ vs $K_{T}, \mathrm{P}$ vs $K_{T}^{\prime}, \quad \mathrm{P}$ vs $-K_{T} K_{T}{ }^{\prime \prime}$ shown in fig. $(1-24)$.
By presenting a comprehensive analysis for EOS in the limit of extreme compression, Stacey [27-28] has given some basic criteria which must be satisfied by an EOS for its validity and applicability. We list these criteria as
(i) In the limit $\frac{V}{V_{0}} \rightarrow 0$, the pressure should not remain finite but it must approach infinity.
(ii) The isothermal bulk modulus must increase regularly and continuously with the increase in pressure such that $K_{T} \rightarrow \infty$ in the limit of infinitely large pressure.
(iii) The pressure derivative of isothermal bulk modulus $K_{T}^{\prime}$ must decreases progressively with the increase in pressure such that $K_{T}^{\prime}$ remains greater than $5 / 3$ in the limit of infinitely large pressure i.e. $P \rightarrow \infty$ and $\frac{V}{V_{0}} \rightarrow 0$.
(iv) $K_{0} K_{0}^{\prime \prime}$ must be negative and will decreases with increase in temperature and $-K_{T} K_{T}^{\prime \prime} \rightarrow 0$ as $P \rightarrow \infty$.
From the fig. $(1-6)$, showing the graph P vs $V / V_{0}$, it is observed that the values of pressure calculated by using equations (1-4) are in good agreement with each other in the entire temperature ranges having a slight deviation at higher temperature above 600 K . Also from fig. $(1-6)$ it is clear that in the limit $\frac{V}{V_{0}} \rightarrow 0$, the pressure should not remain finite but it approaches to infinity. It is also observed that the amount of pressure required for producing the same change in $V / V_{0}$ decreases continuously with increase in temperature. This is related to the fact that the bulk modulus becomes less and the material becomes more compressible at higher temperature. It is also clear from fig. (7-12) that bulk modulus increases with the increase in pressure such that $K_{T} \rightarrow \infty$ in the limit of infinitely large pressure, whereas it decreases with increase in temperature but at higher compressions the rate of decrement in bulk modulus with temperature becomes slow.
Bulk modulus is thus found to depend strongly on pressure as well as temperature. From fig. (13-18) it is also clear that the pressure derivative of isothermal bulk modulus decreases with increase in pressure and when $P \rightarrow \infty, K_{T}^{\prime}$ remains greater than $5 / 3$.

From fig. $(7-24)$ it is observed that for $K_{T}, K_{T}^{\prime}$ and $K_{T} K_{T}^{\prime \prime}$, Holzapfel is distinguished from other three EOS i.e. Brennan Stacey, Shanker, and Vinet as these are in good agreement with each other among all the graphs while Holzapfel curve is differ from them. The basic foundation of Holzapfel EOS depends on single parameter. This one parameter EOS
[29-34], based on the assumption that under very strong compression all solids approaches to the Thomas- Fermi state has a certain degree of predictive capability. Thomas-Fermi state is given by [34]
$P=1003.6\left(\frac{Z}{V}\right)^{\frac{5}{3}}$
Where Z and V are atomic number and molar volume ( $\mathrm{cm}^{3} /$ mole) respectively. Stacey has emphases in a very convincing way that analytical EOS describing the phase transition from zero pressure to infinite pressure. The ThomasFermi state is not valid mainly because parameters appearing in such equations cannot remain unchanged through phase transition.

The validity of equation (1-4) can also be checked by using two well accepted constraints [27, 28]. The first constraint revels that $K_{0} K_{0}^{\prime \prime}$ must be negative i.e. less than zero where as the second constraint revels that the first pressure derivative of isothermal bulk modulus at extreme compression must be greater than or equal to $5 / 3$ i.e. $K_{\infty}^{\prime} \geq 5 / 3$.

The first set of constraints is based on the fact that $K_{T}^{\prime}$ decreases with increase in the pressure, this has been supported theoretically as shown in fig. (13-18).
For second set of constraints, Keane [35-37] and Stacey EOS yields an identical relationship given as

$$
\begin{equation*}
K_{0} K_{0}^{\prime}=-K_{0}^{\prime}\left(K_{0}^{\prime}-K_{\infty}^{\prime}\right) \tag{19}
\end{equation*}
$$

Using the value of $K_{0}^{\prime \prime}$ and $K_{0}^{\prime}$ from Table (2-7), it is observed that the value of $K_{\infty}^{\prime} / K_{0}^{\prime}$ yields a result $\approx 0.9$ which is greater than $3 / 5$ upto 600 K for all the four EOS whereas beyond 600 K Holzapfel equation fails hopelessly to satisfy the constraint $K_{\infty}^{\prime} \geq 5 / 3$.

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Table1: Values of Input parameters of Isothermal bulk modulus $\left(K_{0}\right)$ and its first pressure derivative $\left(K^{\prime}{ }_{0}\right)$ at zero pressure for
NaCl at different temperature $[24,25,26]$.

| S. No. | Temperature $(\mathrm{K})$ | $\mathrm{K}_{0}(\mathrm{GPa})$ | $\mathrm{K}_{0}^{\prime}$ |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 2. | 300 | 24.0 | 5.35 |
| 3. | 450 | 21.6 | 5.51 |
| 4. | 600 | 19.0 | 5.73 |
| 5. | 900 | 16.5 | 6.03 |
| 6. | 1050 | 14.1 | 6.40 |
|  |  | 11.7 | 6.85 |

Table 2: Values of $\mathbf{P}(\mathbf{G P a}), K_{T}(\mathbf{G P a}), K^{\prime}{ }_{T}$ and $K_{T} K^{\prime \prime}{ }_{T}$ calculated by using (A )Holzapfel EOS, (B) Brennan Stacey EOS, (C) Shanker EOS and (D) Vinet EOS for NaCl at 300K.

| $\mathrm{V} / \mathrm{V}_{0}$ | P(A) | P (B) | $\mathrm{P}(\mathrm{C})$ | P(D) | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime} \mathrm{T}^{(A)}$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime} \mathrm{T}^{(B)}$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime}{ }_{\mathrm{T}}(\mathrm{C})$ | $\left.\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime} \mathrm{T}^{(\mathrm{D}}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 24 | 24 | 24 | 24 | 5.35 | 5.35 | 5.35 | 5.35 | -8.30 | -9.04 | -9.04 | -9.30 |
| 0.95 | 1.41 | 1.41 | 1.41 | 1.41 | 31.26 | 31.2 | 31.27 | 31.23 | 4.98 | 4.93 | 4.98 | 4.93 | -6.41 | -7.26 | -7.25 | -7.42 |
| 0.9 | 3.34 | 3.34 | 3.34 | 3.34 | 40.56 | 40.38 | 40.58 | 40.37 | 4.67 | 4.58 | 4.67 | 4.54 | -5.07 | -5.97 | -5.94 | -6.11 |
| 0.85 | 5.99 | 5.97 | 5.99 | 5.97 | 52.56 | 51.98 | 52.57 | 52.02 | 4.41 | 4.27 | 4.4 | 4.29 | -4.07 | -5.00 | -4.96 | -5.04 |
| 0.8 | 9.64 | 9.55 | 9.62 | 9.56 | 68.18 | 66.74 | 68.09 | 66.95 | 4.19 | 3.99 | 4.16 | 4.04 | -3.32 | -4.26 | -4.20 | -3.96 |
| 0.75 | 14.7 | 14.45 | 14.6 | 14.5 | 88.75 | 85.6 | 88.35 | 86.25 | 3.99 | 3.73 | 3.94 | 3.82 | -2.74 | -3.66 | -3.59 | -3.46 |
| 0.7 | 21.7 | 21.17 | 21.5 | 21.3 | 116.2 | 109.83 | 115 | 111.44 | 3.82 | 3.5 | 3.75 | 3.62 | -2.29 | -3.18 | -3.10 | -3.36 |
| 0.65 | 31.6 | 30.43 | 31 | 30.7 | 153.2 | 141.14 | 150.4 | 144.68 | 3.66 | 3.28 | 3.56 | 3.43 | -1.92 | -2.77 | -2.70 | -3.05 |

Table3: Values of of $\mathbf{P}(\mathbf{G P a}), K_{T}(\mathbf{G P a}), K_{T}{ }_{T}$ and $K_{T} K^{\prime \prime}{ }_{T}$ calculated by using (A )Holzapfel EOS, (B) Brennan Stacey EOS, (C) Shanker EOS and (D) Vinet EOS for NaCl at 450K.

| $\mathrm{V} / \mathrm{V}_{0}$ | $\mathrm{P}(\mathrm{A})$ | P(B) | $\mathrm{P}(\mathrm{C})$ | $\mathrm{P}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}$ ( A$)$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime}{ }_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{D})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 21.6 | 21.6 | 21.6 | 21.6 | 5.51 | 5.51 | 5.51 | 5.51 | -8.82 | -9.41 | -9.41 | -9.82 |
| 0.95 | 1.28 | 1.28 | 1.28 | 1.27 | 28.35 | 28.33 | 28.36 | 28.32 | 5.11 | 5.08 | 5.13 | 5.07 | -6.76 | -7.53 | -7.52 | -7.79 |
| 0.9 | 3.04 | 3.03 | 3.04 | 3.03 | 37.04 | 36.9 | 37.08 | 36.87 | 4.79 | 4.71 | 4.8 | 4.71 | -5.31 | -6.18 | -6.15 | -6.39 |
| 0.85 | 5.46 | 5.44 | 5.46 | 5.44 | 48.32 | 47.84 | 48.38 | 47.82 | 4.52 | 4.39 | 4.52 | 4.4 | -4.25 | -5.17 | -5.13 | -5.37 |
| 0.8 | 8.82 | 8.75 | 8.81 | 8.75 | 63.09 | 61.86 | 63.11 | 61.95 | 4.29 | 4.1 | 4.27 | 4.14 | -3.46 | -4.40 | -4.34 | -4.60 |
| 0.75 | 13.5 | 13.31 | 13.4 | 13.3 | 82.63 | 79.89 | 82.45 | 80.31 | 4.08 | 3.83 | 4.1 | 3.91 | -2.85 | -3.79 | -3.72 | -4.01 |
| 0.7 | 20.1 | 19.6 | 19.9 | 19.7 | 108.8 | 103.19 | 108.1 | 104.42 | 3.9 | 3.6 | 3.8 | 3.7 | -2.37 | -3.29 | -3.21 | -3.54 |
| 0.65 | 29.4 | 28.34 | 28.9 | 28.6 | 144.5 | 133.5 | 142.3 | 136.44 | 3.74 | 3.36 | 3.6 | 3.52 | -1.99 | -2.87 | -2.80 | -3.16 |

Table4: Values of $\mathbf{P}(\mathbf{G P a}), K_{T}(\mathbf{G P a}), K^{\prime}{ }_{T}$ and $K_{T} K^{\prime \prime}{ }_{T}$ calculated by using (A )Holzapfel EOS, (B) Brennan Stacey EOS, (C) Shanker EOS and (D) Vinet EOS for NaCl at 600 K .

| V/V ${ }_{0}$ | $\mathrm{P}(\mathrm{A})$ | $\mathrm{P}(\mathrm{B})$ | $\mathrm{P}(\mathrm{C})$ | P (D) | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}^{\prime} \mathrm{T}^{(\mathrm{D}}$ ) | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime}{ }_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{D})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 19 | 19 | 19 | 19 | 5.73 | 5.73 | 5.73 | 5.73 | -9.55 | -9.93 | -9.93 | -10.50 |
| 0.95 | 1.13 | 1.13 | 1.13 | 1.13 | 25.2 | 25.19 | 25.22 | 25.17 | 5.3 | 5.28 | 5.32 | 5.26 | -7.25 | -7.89 | -7.89 | -8.30 |
| 0.9 | 2.69 | 2.7 | 2.7 | 2.7 | 33.24 | 33.14 | 33.31 | 33.09 | 4.96 | 4.89 | 4.98 | 4.88 | -5.65 | -6.46 | -6.43 | -6.76 |
| 0.85 | 4.89 | 4.88 | 4.89 | 4.87 | 43.76 | 43.4 | 43.89 | 43.31 | 4.67 | 4.55 | 4.69 | 4.56 | -4.50 | -5.40 | -5.35 | -5.65 |
| 0.8 | 7.95 | 7.89 | 7.95 | 7.88 | 57.63 | 56.66 | 57.81 | 56.6 | 4.42 | 4.25 | 4.42 | 4.28 | -3.64 | -4.59 | -4.53 | -4.83 |
| 0.75 | 12.2 | 12.1 | 12.2 | 12.1 | 76.13 | 73.87 | 76.25 | 74.82 | 4.21 | 3.98 | 4.19 | 4.04 | -2.99 | -3.96 | -3.88 | -4.20 |
| 0.7 | 18.3 | 17.93 | 18.2 | 18 | 101.1 | 96.31 | 100.9 | 97.07 | 4.02 | 3.72 | 3.97 | 3.83 | -2.48 | -3.44 | -3.36 | -3.71 |
| 0.65 | 27 | 26.13 | 26.6 | 26.2 | 135.4 | 125.78 | 134.1 | 127.93 | 3.85 | 3.48 | 3.78 | 3.63 | -2.08 | -3.00 | -2.93 | -3.30 |

Table 5: Values of of $\mathbf{P}(\mathbf{G P a}), K_{T}(\mathbf{G P a}), K_{T}{ }_{T}$ and $K_{T} K^{\prime \prime}{ }_{T}$ calculated by using (A )Holzapfel EOS, (B) Brennan Stacey EOS, (C) Shanker EOS and (D) Vinet EOS for NaCl at 750K.

| $\mathrm{V} / \mathrm{V}_{0}$ | P(A) | $\mathrm{P}(\mathrm{B})$ | $\mathrm{P}(\mathrm{C})$ | $\mathrm{P}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\left.\mathrm{K}^{\prime} \mathrm{T}_{( } \mathrm{B}\right)$ | $\mathrm{K}^{\prime}{ }_{\mathrm{T}}(\mathrm{C})$ | $\left.\mathrm{K}^{\prime} \mathrm{T}_{( } \mathrm{D}\right)$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime}{ }_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{D})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 16.5 | 16.5 | 16.5 | 16.5 | 6.03 | 6.03 | 6.03 | 6.03 | -10.60 | -10.63 | -10.60 | -11.60 |
| 0.95 | 0.99 | 0.99 | 0.99 | 0.99 | 22.2 | 22.19 | 22.22 | 22.17 | 5.56 | 5.55 | 5.59 | 5.52 | -7.93 | -8.40 | -8.39 | -9.00 |
| 0.9 | 2.38 | 2.38 | 2.38 | 2.38 | 29.67 | 29.61 | 29.76 | 29.53 | 5.18 | 5.14 | 5.23 | 5.1 | -6.12 | -6.80 | -6.81 | -7.30 |
| 0.85 | 4.35 | 4.34 | 4.36 | 4.33 | 39.53 | 39.2 | 39.75 | 39.13 | 4.87 | 4.78 | 4.91 | 4.76 | -4.84 | -5.70 | -5.65 | -6.04 |
| 0.8 | 7.13 | 7.09 | 7.14 | 7.07 | 52.68 | 51.99 | 53.06 | 51.75 | 4.61 | 4.46 | 4.64 | 4.47 | -3.89 | -4.80 | -4.78 | -5.15 |
| 0.75 | 11.1 | 10.97 | 11.1 | 10.9 | 70.4 | 68.69 | 70.91 | 68.47 | 4.38 | 4.17 | 4.39 | 4.21 | -3.18 | -4.20 | -4.10 | -4.46 |
| 0.7 | 16.7 | 16.4 | 16.7 | 16.4 | 94.59 | 90.73 | 95.06 | 90.84 | 4.18 | 3.9 | 4.16 | 3.99 | -2.63 | -3.60 | -3.56 | -3.93 |
| 0.65 | 24.9 | 24.21 | 24.7 | 24.2 | 128.1 | 120 | 128 | 121.14 | 4.01 | 3.65 | 3.95 | 3.78 | -2.20 | -3.20 | -3.12 | -3.49 |

Table 6: Values of $\mathbf{P}(\mathbf{G P a}), K_{T}(\mathbf{G P a}), K_{T}{ }_{T}$ and $K_{T} K^{\prime \prime}{ }_{T}$ calculated by using (A )Holzapfel EOS, (B) Brennan Stacey EOS, (C) Shanker EOS and (D) Vinet EOS for NaCl at 900 K .

| V/V ${ }_{0}$ | $\mathrm{P}(\mathrm{A})$ | P (B) | $\mathrm{P}(\mathrm{C})$ | P (D) | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}$ (B) | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime} \mathrm{T}^{(A)}$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime}{ }_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{D})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 14.1 | 14.1 | 14.1 | 14.1 | 6.4 | 6.4 | 6.4 | 6.4 | -11.90 | -11.50 | -11.50 | -12.90 |
| 0.95 | 0.85 | 0.85 | 0.85 | 0.85 | 19.3 | 19.31 | 19.33 | 19.28 | 5.88 | 5.88 | 5.93 | 5.83 | -8.79 | -9.00 | -8.99 | -9.90 |
| 0.9 | 2.07 | 2.08 | 2.08 | 2.07 | 26.21 | 26.21 | 26.34 | 26.09 | 5.46 | 5.44 | 5.53 | 5.38 | -6.71 | -7.30 | -7.26 | -7.90 |
| 0.85 | 3.83 | 3.82 | 3.84 | 3.81 | 35.46 | 35.38 | 35.78 | 35.1 | 5.12 | 5.06 | 5.2 | 5.01 | -5.25 | -6.10 | -6.02 | -6.53 |
| 0.8 | 6.34 | 6.33 | 6.37 | 6.29 | 47.94 | 47.58 | 48.55 | 47.1 | 4.84 | 4.72 | 4.9 | 4.7 | -4.19 | -5.20 | -5.09 | -5.53 |
| 0.75 | 9.96 | 9.9 | 10 | 9.83 | 64.97 | 63.88 | 65.96 | 63.1 | 4.59 | 4.41 | 4.63 | 4.43 | -3.41 | -4.50 | -4.37 | -4.78 |
| 0.7 | 15.2 | 15.04 | 15.3 | 14.9 | 88.52 | 85.75 | 89.87 | 85.06 | 4.38 | 4.12 | 4.39 | 4.19 | -2.81 | -3.90 | -3.80 | -4.20 |
| 0.65 | 22.9 | 22.44 | 22.9 | 22.3 | 121.6 | 115.24 | 123 | 115.06 | 4.19 | 3.85 | 4.16 | 3.97 | -2.34 | -3.40 | -3.34 | -3.73 |

Table7: Values of $\mathbf{P}(\mathbf{G P a}), K_{T}(\mathbf{G P a}), K^{\prime}{ }_{T}$ and $K_{T} K^{\prime \prime}{ }_{T}$ calculated by using (A )Holzapfel EOS, (B) Brennan Stacey EOS, (C) Shanker EOS and (D) Vinet EOS for NaCl at 1050 K

| V/V ${ }_{0}$ | $\mathrm{P}(\mathrm{A})$ | $\mathrm{P}(\mathrm{B})$ | $\mathrm{P}(\mathrm{C})$ | P (D) | KT(A) | $\mathrm{K}_{\mathrm{T}}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{A})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{B})$ | $\mathrm{K}_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}}^{\prime}(\mathrm{D})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}$ ( A$)$ | $\left.\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime} \mathrm{T}^{(\mathrm{B}}\right)$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime}{ }_{\mathrm{T}}(\mathrm{C})$ | $\mathrm{K}_{\mathrm{T}} \mathrm{K}^{\prime \prime}{ }_{\mathrm{T}}(\mathrm{D})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | 11.7 | 11.7 | 11.7 | 11.7 | 6.85 | 6.85 | 6.85 | 6.85 | -13.60 | -12.54 | -12.50 | -14.60 |
| 0.95 | 0.71 | 0.72 | 0.72 | 0.71 | 16.36 | 16.38 | 16.4 | 16.34 | 6.26 | 6.28 | 6.33 | 6.21 | -9.80 | -9.72 | -9.71 | -11.00 |
| 0.9 | 1.76 | 1.76 | 1.77 | 1.76 | 22.65 | 22.7 | 22.82 | 22.54 | 5.79 | 5.81 | 5.91 | 5.71 | -7.42 | -7.83 | -7.80 | -8.70 |
| 0.85 | 3.29 | 3.3 | 3.31 | 3.28 | 31.19 | 31.27 | 31.63 | 30.88 | 5.42 | 5.41 | 5.54 | 5.31 | -5.75 | -6.50 | -6.45 | -7.12 |
| 0.8 | 5.52 | 5.53 | 5.57 | 5.48 | 42.9 | 42.91 | 43.8 | 42.16 | 5.11 | 5.04 | 5.22 | 4.97 | -4.55 | -5.52 | -5.45 | -5.99 |
| 0.75 | 8.79 | 8.79 | 8.81 | 8.67 | 59.14 | 58.78 | 60.71 | 57.56 | 4.85 | 4.71 | 4.93 | 4.68 | -3.68 | -4.77 | -4.69 | -5.17 |
| 0.7 | 13.6 | 13.56 | 13.8 | 13.3 | 81.95 | 80.48 | 84.39 | 78.8 | 4.62 | 4.4 | 4.67 | 4.43 | -3.02 | -4.57 | -4.10 | -4.50 |
| 0.65 | 20.8 | 20.29 | 21 | 20.2 | 114.5 | 110.33 | 117.9 | 108.44 | 4.41 | 4.11 | 4.42 | 4.2 | -2.51 | -3.68 | -3.61 | -4.02 |

Fig.(1-6) :Plots of compressions $\mathrm{V} / \mathrm{V}_{\mathbf{0}}$ vs $\mathbf{P}$ for NaCl by using equations (1-4) at different temperature.



Fig. (7-12): Plots of pressure $\mathbf{P}$ vs $\mathbf{K}_{\mathbf{T}}$ for NaCl by using equations (5-8) at different temperature.

Fig. 7 NaCl at 300K





Fig. (13-18): Plots of pressure P vs $K_{T}^{\prime}$ for NaCl by using equations (10-13) at different temperature.






Fig. (19-24): Plots of pressure $\mathbf{P}$ vs $-K_{T} K_{T}^{\prime \prime}$ for NaCl by using equations (14-17) at different temperature.






