Available online at www.elixirpublishers.com (Elixir International Journal)

Mechanical Engineering



Elixir Mech. Engg. 62 (2013) 17555-17563

Demand estimation for a short life cycle and novel product by using modified Markov based algorithm

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ARTICLE INFO

Article history: Received: 10 July 2013; Received in revised form: 20 August 2013; Accepted: 2 September 2013;

Keywords Demand, Markov Chain, Algorithm, Optimization, Short life cycle, Supply chain, Basic exponential smoothing.

ABSTRACT

This paper deals with demand prediction by combining basic exponential smoothening with Markov based algorithm. This demand prediction is suitable for novel and minimum shelf life products and is suited for small scale retailers and manufacturers, since for them acquisition of costly software tools is out of their financial reach. This paper attempts to arrive at predicting a fixed value of demand which will enhance the profit. The Exponential smoothing process involves comparing the latest observation with the previous weighted average and making a proportional adjustment, governed by the coefficient α , known as the smoothing constant. By convention we constrain the coefficient to the range, so that only a part of the difference between the old mean and the new observation is used in the updating, $0 < \alpha < 1$.Initially demand is predicted by using basic exponential smoothing for two successive months and error of demand for each day is estimated. Markov based algorithm is then applied for these errors and the steady state probability is then determined for each state. The demand corresponding to the state with maximum probability is taken as the optimum one and the corresponding profit is estimated. This concept is then implemented for a baked product and the annual savings for a particular product is then established.

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Introduction

In Short life cycle Product the demand forecast error of supplier or manufacture is generally between 40 - 100% [2]. Actually, with the quick development of science and technology and with continuous rise of peoples demand more and more products will have the characteristic of short life cycle. This phenomenon will play more in the commodity market of fierce competition. The main reasons are 1. Speed of technology refreshing is more and more 2. The consumption is more and more of short life characteristic [3]. Many researchers in the field of logistics analyzed the returning goods problem of short life cycle product. Most investigated impact of supply chain management on logistical performance indicators in food supply chains especially in the case of baked products[4]. Lee found that product that has not been sold at the end of the season may be either returned to the manufacturer or processed at the discount shop [5]. The above problems as stated in the literature gives as an opportunity to analyze the demand estimation of short life cycle product supply chain.

Agrawal and Smith used negative binomial distribution (NBD) for the demand model and suggested that NBD model provides a better fit than the normal or Poisson distributed data [6]. Cachon used the negative binomial distribution model to analyze the demand of the fashion goods where it is assumed that the demand process follows the Poisson distribution and demand rate varies according to a gamma distributed model [7]. Hammond studied the Quick Response policy with ski apparel (ski suits, ski pants, parkas, etc), and showed that forecast accuracy can be substantially improved by adopting QR policy [11]. A Markov chain model is a stochastic process, with discrete states and continuous time in which modeling is done on observable parameters. This model can be utilized to evaluate the probability of different states with respect to time. The earlier states are irrelevant for predicting the following states, since the current state is known [19]. In 2001, Zhang and He have developed a Grey–Markov forecasting model for forecasting the total power requirement of agricultural machinery in Shangxi Province [21]. In 2007, Akay and Atak have formulated a Grey prediction model with rolling mechanism for electricity demand forecasting of Turkey [22]. A Grey–Markov forecasting model has been developed by Huang, He and Cen in 2007. The Markov-chain forecasting model is applicable to problems with random variation, which could improve the GM forecasting model [23]. Bijesh and Jayadas formulated an algorithm for short life cycle supply chain based on Markov model [24]. The above algorithm gives us a useful and financially feasible technique to determine the demand forecast whenever the demand data given is randomly distributed

Basic Exponential Smoothing (BES)

Nice properties of a weighted moving average would be one where the weights not only decrease as older and older data are used, but one where the differences between the weights are "smooth". Obviously the desire would be for the

weight on the most recent data to be the largest. The weights should then get progressively smaller the more periods one considers into the past. The exponentially decreasing weights of the basic exponential smoothing forecast fit this bill nicely. The forecast equation is given by:

 $F_{t+1} = \alpha D_t + (1 - \alpha) F_t$, Where α is a smoothing parameter between 0 and 1. Here we assume $\alpha = .2$.

Also Forecasting Error = $E_t = (F_t - D_t)$

Methodology

1. Observed demand data for a short life cycle product is collected for any two successive months.

2. Apply B.E.S to the collected data and estimate the errors in forecasting for all the days of two successive months

3. Implement the generalized algorithm for the errors of the forecasted model

4. Deduce the initial probability matrix and the Transition probability matrix for the different states of errors of demand.

5. By utilizing the above two matrices the probability of different states of demand for any future period can be determined. The evolution of the system is determined by multiplying the transition matrix by the previous state vector (probability matrix), which is a stochastic vector representing the probabilities of the system being in any one of the given states

6. Choose the state with maximum probability from the obtained current probability vector

7. Determine the annual savings by adopting the demand of the state with maximum probability.

Algoritm for modification of demand forecsting of basic exponential smoothing method by using markov based algorithm

1) Collect the observed data for sales of a particular product with minimum shelf life for any two consecutive or successive months, say t and t+1

2) Apply B.E.S to the collected data and estimate the errors in forecasting for all the days of two successive months

3).Determine the upper limit and lower limit of the errors in forecasting by B.E.S for the tth month. Determine the range or band width of the error as the difference between upper limit and lower limit for the tth month

4) Discretize the obtained range into states or class intervals with minimum possible no of sample size. Let us denote these states as $X_1 X_2 X_3 \dots X_n$

5) Determine the initial probability vector P^0 for the month t. This matrix gives the initial probability of all states say $X_1, X_2, X_3, \ldots, X_n$ in month t.

a) List out all the days (m) in a month in the month t as the first column, in the ascending order of the table

b) In second column enter the state of the observed error for all the days of tth month listed in the first column

c) Count the no of occurrence of each state in tth month. (For eg say state X_i is occurring j times in the month t of m days, then initial probability of $X_i = j/m$)

d) Determine the initial probability of all states by using the formulae $X_i = J/M$ where J is the occurrence of ith state in tth month of M days and i= 1, 2, 3....n.

e) Represent the initial probabilities obtained from step 8 as a row vector (1*n) with n no of entries and is called as initial probability vector denoted by P^0 .

6) Construct state occurrence table for tth month and t+1th month.

a) List out all the days of t^{th} and $t+1^{th}$ month in the ascending order as the first column of the table. Assume the number of working days in both months as same

b) In the second column of the table enter the state corresponding to errors in forecasting for all the days listed in t^{th} month.

c) In column three enter the state corresponding to errors of forecasting for all days listed in the t+1th month.

7) Deduce transition probability matrix from the event occurrence table.

a) Any current state X_i in a particular day of tth month can transform into states $X_{1,}X_{2,}X_{3,}...X_n$ during the same day of t+1th month. Hence there exits n probabilities which results from the probable transformation of current state X_i to other possible states $X_{1,}X_{2,}X_{3,}...X_n$. Represent these probabilities as P_{11} , $P_{12,...,P_{1n}}$

b) Form the Transition probability matrix by representing all the current states as rows and next states as columns. Now enter the probabilities as P_{11} , P_{12} , P_{1n} in 1st row and repeat the same procedure for other rows. Any entry say P_{ij} = No of transformations of current state i of tth month in a particular day to next state j of t+1 th month in the same day/ Total no of occurrence of current state i in the tth month

8) Deduce the current probability vector for the succeeding months t+2, t+3 as

 $P^{1}=P^{0}* TPM$ $P^{2}=P^{1}* TPM$

 $P^{m} = P^{m-1} * TPM$

9) Choose the state with maximum probability from the obtained current probability vector for say the mthmonth which is a row matrix with probability of each state during say mthmonth.

10) Determine the possible profit to firm by the adoption of this state of production as indicated by the step 8

Implementation of the Proposed Algorithm For A Baked Product

Step-1

The data collected from a reputed baking firm is furnished below. The firm has been producing 1300 items per day and selling this item @ Rs 12. Any leftover item is sold at a rate of Rs 3 and there by occurring a possible loss of profit of Rs 9 per product for left over item. Cost of each item is Rs7. This data is manipulated by using naïve forecasting and the forecast as well as error for all the days of April and May is estimated.

Table-1							
		$F_{t+1} =$	Error =				Error =
		$.2D_t + .8F_t$	$E_t =$			$F_{t+1} =$	$(F_t - D_t)$
			$(\mathbf{F}_{t} - \mathbf{D}_{t})$	Demand		$.2D_t + .8F_t$	May
Demand D	Mean X _m		April	X	Mean X _m		
1260	1263.74	1263.74	3.74	1260	1263.74	1265.396	5.396264
1267	1263.74	1262.99	-4.008	1260	1263.74	1264.317	4.317011
1260	1263.74	1263.79	3.7936	1268	1263.74	1263.454	-4.54639
1252	1263.74	1263.035	11.03488	1255	1263.74	1264.363	9.362887
1248	1263.74	1260.828	12.8279	1249	1263.74	1262.49	13.49031
1266	1263.74	1258.262	-7.73768	1267	1263.74	1259.792	-7.20775
1271	1263.74	1259.81	-11.1901	1267	1263.74	1261.234	-5.7662
1260	1263.74	1262.048	2.047887	1265	1263.74	1262.387	-2.61296
1259	1263.74	1261.638	2.638309	1265	1263.74	1262.91	-2.09037
1264	1263.74	1261.111	-2.88935	1268	1263.74	1263.328	-4.6723
1256	1263.74	1261.689	5.688518	1259	1263.74	1264.262	5.262164
1265	1263.74	1260.551	-4.44919	1267	1263.74	1263.21	-3.79027
1260	1263.74	1261.441	1.440652	1264	1263.74	1263.968	-0.03222
1271	1263.74	1261.153	-9.84748	1269	1263.74	1263.974	-5.02577
1265	1263.74	1263.122	-1.87798	1271	1263.74	1264.979	-6.02062
1271	1263.74	1263.498	-7.50239	1265	1263.74	1266.184	1.183506
1259	1263.74	1264.998	5.998091	1262	1263.74	1265.947	3.946805
1266	1263.74	1263.798	-2.20153	1268	1263.74	1265.157	-2.84256
1270	1263.74	1264.239	-5.76122	1269	1263.74	1265.726	-3.27405
1260	1263.74	1265.391	5.391023	1263	1263.74	1266.381	3.380764
1262	1263.74	1264.313	2.312818	1268	1263.74	1265.705	-2.29539
1268	1263.74	1263.85	-4.14975	1265	1263.74	1266.164	1.163689
1265	1263.74	1264.68	-0.3198	1260	1263.74	1265.931	5.930951
1271	1263.74	1264.744	-6.25584	1269	1263.74	1264.745	-4.25524
1263	1263.74	1265.995	2.99533	1265	1263.74	1265.596	0.595809

Error in demand data modified to nearest whole no. Table-2

Date	Error of Demand during each day of April 2012	Error of Demand during each day of May 2012
01-04-2012	4	5
02-04-2012	-4	4
03-04-2012	4	-5
04-04-2012	11	9
05-04-2012	13	13
06-04-2012	-8	-7
07-04-2012	-11	-6
08-04-2012	2	-3
09-04-2012	3	-2
10-04-2012	-3	-5
11-04-2012	6	5
12-04-2012	-4	-4

13-04-2012	1	0
14-04-2012	-10	-5
15-04-2012	-2	-6
16-04-2012	-8	1
17-04-2012	6	4
18-04-2012	-2	-3
19-04-2012	-6	-3
20-04-2012	5	3
21-04-2012	2	-2
22-04-2012	-4	1
23-04-2012	0	6
24-04-2012	-6	-4
25-04-2012	3	1

Step-2

The Range = Highest error in demand – Lowest error in Demand =13- (-11) = 24. Step 3

Discretize the range into class intervals or states with a minimum sample size of 3. I.e. Say 8 states denoted by $X_{1,1}X_{2,2}$, $X_{3,1}$, $X_{3,2}$,

Step 4

Determine the initial probability vector P^0 for the month April. This matrix gives the initial probability of all states say $X_1 X_2 X_3 \dots X_8$ in the month of April.

Table-3							
Class interval of error of demand	State	No of occurrence	Probability				
-11,-10,-9	X ₁	2	.08				
-8,-7,-6	X ₂	4	.16				
-5,-4,-3	X ₃	4	.16				
-2,-1,0	X_4	3	.12				
1,2,3	X ₅	5	.2				
4,5,6	X ₆	5	.2				
7,8,9	X ₇	0	0				
10,11,12,13	X ₈	2	.08				

The Fourth row of the above table gives initial probability vector P^0 for the month April. This matrix gives the initial probability of all states say $X_{1,1}X_{2,1}X_{3,1}$ X_8 in the month of April.

 $\mathbf{P}^{0} = [.08, .16, .16, .12, .2, .2, 0, .08]$

Step 5 – State transition table

Table -4							
Day	Current state (April)	Subsequent state (May)					
1	6	6					
2	4	6					
3	6	3					
4	8	7					
5	8	8					
6	2	2					
7	1	2					
8	5	3					
9	5	4					
10	4	4					
11	6	6					
12	3	3					
13	5	4					
14	1	3					
15	4	2					
16	2	5					
17	6	6					

18	4	3
19	2	3
20	6	5
21	5	4
22	3	5
23	4	6
24	2	3
25	5	5

Step 6

Deduction of Transition Probability Matrix (T P M)

. Any current state X_i in a particular day of tth month can transform into states $X_1, X_2, X_3, \ldots, X_n$ during the same day of t+1th month. Hence there exits n probabilities which results from the probable transformation of current state X_i to other possible states $X_1, X_2, X_3, \dots, X_n$ Represent these probabilities as $P_{11}, P_{12}, \dots, P_{1n}$ • Form the Transition probability matrix by representing all the current states as rows and next states as columns. Now

enter the probabilities as P_{11} , P_{12} , P_{1n} in 1st row and repeat the same procedure for other rows. • Any entry say P_{ij} = No of transformations of current state i of t th month in a particular day to next state j of t+1th month in the same day/ Total no of occurrence of current state i in the tth month

Transition Probability Matrix,

rable-5	Tabl	e	-5
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	1	2	3	4	5	6	7	8
1	0	.5	.5	0	0	0	0	0
2	0	.25	.5	0	.25	0	0	0
3	0	0	.5	0	.5	0	0	0
4	0	.2	.2	.2	0	.4	0	0
5	0	0	.2	.6	.2	0	0	0
6	0	0	.2	0	.2	.6	0	0
7	0	0	0	0	0	0	0	0
8	0	0	0	0	0	0	.5	.5

Step 7

Deduce the current probability vector for the succeeding month's t+2, t+3t+18as $P^{1=}P^{0*}TPM = [0 \ 0.1040 \ 0.3040 \ 0.1440 \ 0.2000]$ 0.1680 0.0400 0.0400] 0.1584 $P^2 = [0]$ 0.0548 0.3064 0.1488 0.2516 0.0200 0.0200] $P^{3} = [0]$ 0.0435 0.2924 0.1807 0.2489 0.1546 0.0100 0.0100] $P^4 = [0]$ 0.0470 0.2847 0.1855 0.2377 0.1650 0.0050 0.0050] $P^5 = [0]$ 0.0488 0.2835 0.1797 0.2347 0.1732 0.0025 0.0025] 0.2837 0.2356 $P^6 = [0]$ 0.0482 0.1768 0.1758 0.0013 0.0013] $P^7 = [0]$ 0.0474 0.2836 0.1767 0.2362 0.1762 0.0006 0.0006] $P^8 = [0]$ 0.2833 0.0472 0.1770 0.2361 0.1764 0.0003 0.0003] $P^9 = [0]$ 0.0472 0.2831 0.1771 0.2359 0.1766 0.0002 0.0002] $P^{10} = [0]$ 0.0472 0.2831 0.2359 0.1770 0.1768 0.0001 0.0001] $P^{11} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000 0.0000] $P^{12} = [0]$ 0.2831 0.1769 0.2359 0.0472 0.1769 0.0000 0.0000] $P^{13} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000 0.0000] $P^{14} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000 0.0000] $P^{15} = [0]$ 0.0472 0.2831 0.2359 0.1769 0.1769 0.0000 0.0000] $P^{16} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000 0.0000] $P^{17} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000 0.0000] $P^{18} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000] 0.0000 $P^{19} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000 0.00001 $P^{20} = [0]$ 0.0472 0.2831 0.1769 0.2359 0.1769 0.0000 0.0000] Step 8

The maximum Probability is for state 3 and as time passes we can see that probability of demand for state 1 is approaching steady state probability. The Probability V/s Time curve for state one is shown below



Step 9

The maximum probability is for state 3 with errors -5,-4,and-3. The corresponding demands are 1267, 1264, 1265 and 1268. To determine the single point estimate of demand, the annual profit by adopting each of the above figures of demand are determined. The demand with maximum profit is selected as the optimum forecast. For this purpose we are assuming an overstocking cost of (Rs 7-3) =Rs 4 per item and under stocking cost of Rs 5 per piece. The firm was producing 1300 items per day.

Case-1 Assuming predicted demand as 1267 items per day.

Actual Demand for	Predicted demand based on algorithm	Error for demand in	Overstocking cost	Under stocking cost
April.	for April	April	(Rs)	(Rs)
1260	1267	-7	28	
1267	1267	0		
1260	1267	-7	28	
1252	1267	-15	60	
1248	1267	-19	72	
1266	1267	-1	4	
1271	1267	4		20
1260	1267	-7	28	
1259	1267	-8	32	
1264	1267	-3	12	
1256	1267	-11	44	
1265	1267	-2	8	
1260	1267	-7	28	
1271	1267	4		20
1265	1267	-2	8	
1271	1267	4		20
1259	1267	-8	32	
1266	1267	-1	4	
1270	1267	3		15
1260	1267	-7	28	
1262	1267	-5	20	
1268	1267	1		5
1265	1267	-2	8	
1271	1267	4		20
1263	1267	-4	16	
	1267		TOTAL-460	TOTAL-100

Annual Savings by adopting a demand of 1267 items = $\{(1300-1267) (7-3) 24 - 100-460\}12$ = Rs 32880

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Actual Demand for	Predicted demand based on algorithm	Error for demand in	Overstocking cost	Under stocking cost
April.	for April	April	(Rs)	(Rs)
1260	1264	-4	16	
1267	1264	3		15
1260	1264	-4	16	
1252	1264	-12	48	
1248	1264	-16	64	
1266	1264	2		10
1271	1264	7		35
1260	1264	-4	16	
1259	1264	-5	20	
1264	1264	0		
1256	1264	-8	32	
1265	1264	1		5
1260	1264	-4	16	
1271	1264	7		35
1265	1264	1		5
1271	1264	7		35
1259	1264	-5	20	
1266	1264	2		10
1270	1264	6		30
1260	1264	-4	16	
1262	1264	-2	8	
1268	1264	4		20
1265	1264	1		5
1271	1264	7		35
1263	1264	-1	4	
			TOTAL-276	TOTAL-240

Case-2 Assuming predicted demand as 1264 items per day.

Annual Savings by adopting a demand of 1264 items = $\{(1300-1264) (7-3) 24 - 276-240\}12$ = Rs 35280 Case-3

Assuming	predicted	demand	as	1265	items	per	day.
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Actual Demand for	Predicted demand based on algorithm	Error for demand in	Overstocking cost	Under stocking cost
April.	for April	April	(Rs)	(Rs)
1260	1265	-5	20	
1267	1265	2		10
1260	1265	-5	20	
1252	1265	-13	52	
1248	1265	-17	68	
1266	1265	1		5
1271	1265	6		30
1260	1265	-5	20	
1259	1265	-6	24	
1264	1265	-1	4	
1256	1265	-9	36	
1265	1265	0		
1260	1265	-5	20	
1271	1265	6		30
1265	1265	0		
1271	1265	6		30
1259	1265	-6	24	
1266	1265	1		5
1270	1265	5		25
1260	1265	-5	20	
1262	1265	-3	12	
1268	1265	3		15
1265	1265	0		

1271	1265	6		30
1263	1265	-2	8	
			TOTAL-328	Total-180

Annual Savings by adopting a demand of 1264 items = $\{(1300-1265) (7-3) 24 - 328-180\}12$ = Rs 34224 Case-4

Assuming predicted demand as 1268 items per day.

Actual Demand for	Predicted demand	Error for demand in	Overstocking cost	Under stocking cost
April.	based on algorithm	April	(Rs)	(Rs)
	for April			
1260	1268	-8	32	
1267	1268	-1	4	
1260	1268	-8	32	
1252	1268	-16	64	
1248	1268	-20	80	
1266	1268	-2	8	
1271	1268	3		15
1260	1268	-8	32	
1259	1268	-9	36	
1264	1268	-4	16	
1256	1268	-12	48	
1265	1268	-3	12	
1260	1268	-8	32	
1271	1268	3		15
1265	1268	-3	12	
1271	1268	3		15
1259	1268	-9	36	
1266	1268	-2	8	
1270	1268	2		10
1260	1268	-8	32	
1262	1268	-6	24	
1268	1268	0		
1265	1268	-3	12	
1271	1268	3		15
1263	1268	-5	20	
			TOTAL-540	TOTAL-70

Annual Savings by adopting a demand of 1264 items = $\{(1300-1268) (7-3) 24 - 540-70\}12$ = Rs 31080.

Result

The maximum probability is for state 3 with errors -5,-4, and-3. The corresponding demands are 1267, 1264, 1265 and 1268. To determine the single point estimate of demand, the annual profit by adopting each of the above figures of demand are determined. The demand with maximum profit is selected as the optimum forecast. For this purpose we are assuming an overstocking cost of (Rs 7-3) =Rs 4 per item and under stocking cost of Rs 5 per piece. The firm was producing 1300 items per day. The annual savings for each product is determined for each demand stated above by using the formulae {(P-D_f) (E-S)*25- \sum Under stocking costs- \sum Overstocking costs}*12, where P= Production rate per day, D_f is the predicted value of demand by using algorithm, E is the cost of making unit quantity, S is the price of the product after discount to be sold after 8pm. The demand with maximum savings is chosen as the optimal one.

Annual Savings by adopting a demand of 1267 items = $\{(1300-1267) (7-3) 24 - 100-460\}12$ = Rs 32880 Annual Savings by adopting a demand of 1264 items = $\{(1300-1264) (7-3) 24 - 276-240\}12$ = Rs 35280

Annual Savings by adopting a demand of 1265 items = $\{(1300-1265) (7-3) 24 - 328-180\}12$ = Rs 34224

Annual Savings by adopting a demand of 1268 items = $\{(1300-1268) (7-3) 24 - 540-70\}12$ Rs 31080.

The optimal predicted demand with maximum savings is 1264 items.

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