



## Investigation on material removal rate in Abrasive water jet machining

A. S. Patel\* and P. D. Patil

Department of Mechanical Engineering, D. N. Patel college of Engineering, Shahada.

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### ABSTRACT

The AWJM is widely used to process the different materials. The material considered for the experimental study is commercial aluminum, mild steel and EN8. The operating parameters, namely pressure, cutting speed and abrasive flow rate are varied during to find its effect on metal removal rate. Attempt is made to establish relationship between operating parameters and material removal rate by using regression analysis & ANOVA. Experimental study is performed to validate the results. It is observed that pressure & abrasive flow rate are the most significant parameters that affect the material removal rate in AWJM.

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### Introduction

Abrasive Water jet (AWJ) Machining is a recent non-conventional machining process. In this technology, a very high-pressure beam of water and abrasives is used for machining. This technology is used in industry as it has many advantages.

Studied mechanism and effectiveness of material removal process. Different materials were found to possess different material removal rates in machining [1].

It was found that process variables such as pressure, abrasive mass flow rates, traverse rate influence morphology of cutting surface [2].

Material removal process was studied. In first zone the mode of material removal is by micro cutting and intergranular fracture due to impact of abrasive particles at shallow angles. In second zone the mode of material removal is by plastic deformation and intergranular fracture [3]. It was also found that there were no heat damage zones, and no mechanical deformation of work piece due to cutting forces and this is an environmentally friendly process [4].

Kerf geometry is ultimately dependent on the variation of standoff distance, abrasive particle velocity distribution and their local impact angle accounted across the jet foot print [5]. Decreasing the SOD and traverse rate may improve the machining performance [6].

### Experimentation

Experimentation was carried out with objective to establish relationship between Material removal rate (MRR) and operator controlled parameters. Effort was also made to identify the significant parameters affecting MRR. Experimentation was carried out at M/s Ainnovative International Co. Ltd. at Ahmadabad.

The following steps were taken for carrying out the experimentation.

1. Selection of work material.
2. Selection of "parameters to be varied" and "parameters to be kept constant".
3. A set of experiments was conducted to establish regression equation.
4. A set of validation experiments was conducted to check validity of regression equation developed in step no 3

The material selected for experimentation was Aluminum, Mild steel and EN8, which are commercially used in industries for manufacturing various machine parts.

### Machine Used for Experimentation



Figure 1. Abrasive Water Jet Machine

DWJ1525-BB high-pressure system figure 1 is designed and manufactured by M/s Ainnovative international Pvt. Ltd Ahmedabad in collaboration with M/s Dardi, Italy.

### Input Parameters Varied

1. Pressure
2. Cutting Speed
3. Abrasive Flow Rate

**Above parameters are selected because these parameters are operator controlled.**

### Input Parameter Kept Constant

1. Standoff Distance
2. Abrasive Material / Size
3. Orifice Diameter
4. Focusing Tube Diameter / Length

**Above parameters are machine parameters which are not frequently changed**

The main output parameter is material removal rate (MRR) for various combination of factor.

The experimentation was conducted in two sets.

The first set of experiment was conducted for 12 runs for calculating the regression equation. In this runs the parameters are set for level of parameter as 3x2x2.

The second set of experiment was conducted for 6 runs for validation test of regression equation.

**Table 1. Material used for Experiment**

Sr. No.	Material	Length	Width	Thickness
		mm	mm	mm
1	Aluminum	140	100	30
2	Mild steel	145	110	20
3	EN8	200	130	16

**Experiment on Aluminum Plate:**



**Figure 3. Experiment on Aluminum plate**

**Parameters for Training data for regression equation in Aluminum plate**

Factor 1 Pressure Mpa – Level 1 - 180, Level 2 - 210, Level 3 - 240

Factor 2 Cutting Speed mm/min- Level 1 - 100, Level 2 - 150

Factor 3 Abrasive Flow Rate gm/min – Level 1 - 300, Level 2 – 600

**Parameters for validation test in Aluminum plate**

Factor 1 Pressure Mpa – Level 1- 180, Level 2 -210, Level 3 - 240

Factor 2 Cutting Speed mm/min - Level 1 -125

Factor 3 Abrasive Flow Rate gm/min – Level 1-300, Level2– 600

**Experimental Data and Calculations on Aluminum Plate:**

**Table 2. Experiment No-1 Summary Data for Regression Equation**

Sr. No.	Pressure	Cutting speed	AFR	Average kerf	Average DOC
	Mpa	mm/min	gm/min	mm	mm
1	180	150	600	0.91	9.3397
2	180	150	300	0.8775	7.9989
3	180	100	600	1.0525	11.4345
4	180	100	300	0.8975	10.335
5	210	150	600	0.9025	12.747
6	210	150	300	0.8675	10.6957
7	210	100	600	0.9325	18.2966
8	210	100	300	0.9125	16.2177
9	240	150	600	0.9275	16.4729
10	240	150	300	0.8725	14.7071
11	240	100	600	0.94	23.5082
12	240	100	300	0.925	20.6251

**Table 3. Experiment No 2: Summary Data of Depth of Cut for Validation Test**

Sr. No.	Pressure	Cutting Speed	AFR	Average KERF	Average DOC
	Mpa	mm/min	gm/min	mm	mm
1	180	125	600	0.925	11.0449
2	180	125	300	0.86	9.6951
3	210	125	600	0.9125	15.1777
4	210	125	300	0.89	12.9894
5	240	125	600	0.9375	18.8129
6	240	125	300	0.87	17.1056

**Table 4. Experiment No-1: Calculated Data for Regression Equation**

Sr. No.	Pressure	Cutting Speed	AFR	Average Kerf	Average DOC	Exp MRR
	Mpa	mm/min	gm/min	mm	mm	mm <sup>3</sup> /min
1	180	150	600	0.91	9.3397	1274.869
2	180	150	300	0.8775	7.9989	1052.855
3	180	100	600	1.0525	11.4345	1203.481
4	180	100	300	0.8975	10.335	927.5663
5	210	150	600	0.9025	12.747	1725.625
6	210	150	300	0.8675	10.6957	1391.778
7	210	100	600	0.9325	18.2966	1706.158
8	210	100	300	0.9125	16.2177	1479.865
9	240	150	600	0.9275	16.4729	2291.792
10	240	150	300	0.8725	14.7071	1924.792
11	240	100	600	0.94	23.5082	2209.771
12	240	100	300	0.925	20.6251	1907.822

**Regression Analysis for Aluminum plate**

Multiple regression analysis is performed to establish relationship between MRR and pressure, cutting speed and abrasive flow rate. Confidence interval of 95% is used. For calculation MINITAB statistical software is used. An empirical equation is derived to describe the functional relationship between the Material removal rate (MRR) and the pressure, traverse feed, abrasive flow rate parameters.

**Regression Analysis: for Aluminum plate**

The regression equation is

$$\text{Exp MRR} = -2326 + 16.1 \text{ Pressure} + 0.757 \text{ Cutting Speed} + 0.959 \text{ AFR} \text{----(1)}$$

**Table 5. Estimated Regression Coefficient for MRR**

Sr.No	Predictor	Coef	SE Coef	T	P
1	Constant	-2326.0	146.0	-15.93	0.000
2	Pressure	16.1475	0.5723	28.21	0.000
3	Cutting Speed	0.7568	0.5608	1.35	0.214
4	A F R	0.95945	0.09346	10.27	0.000

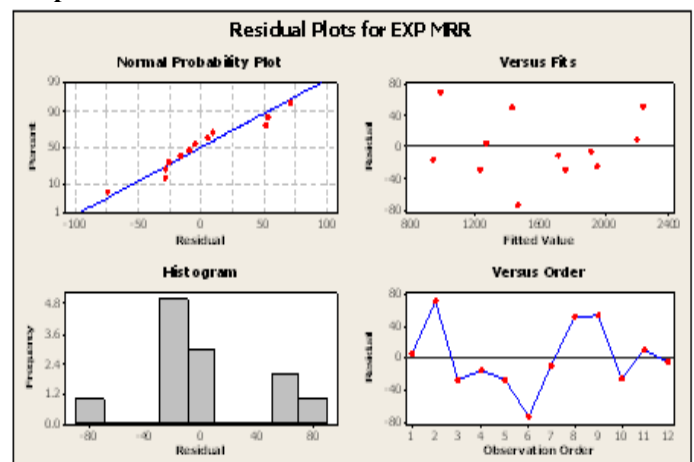
S = 48.5634 R-Sq = 99.1% R-Sq(adj) = 98.8%

**Table 6. Analysis of Variance for MRR**

Sr.No	Source	DF	SS	MS	F	P
1	Regression	3	2130191	710064	301.08	0.000
2	Residual Error	8	18867	2358	---	---
3	Total	11	2149058	---	---	---

**Comments on % error:** The maximum error is 8.5% and average error of prediction is 1.056. The span of error is 11%. This indicates that model is able to predict the outcome with reasonable accuracy.

**Graphs for Aluminum Plate**



**Figure 4. Residual plots**

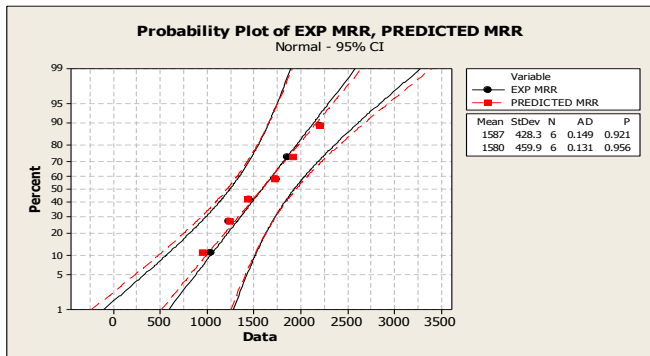


Figure 5. Probability plots

Experiment on Mild Steel Plate:

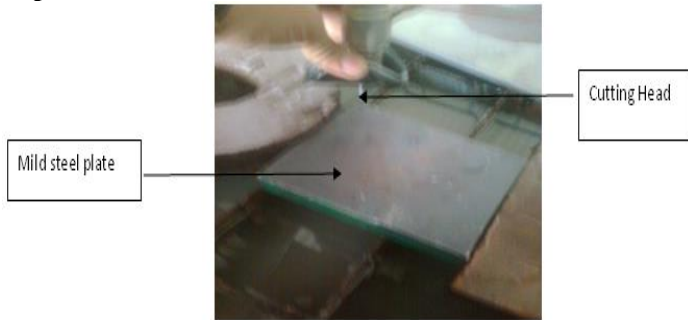


Figure 5. Experiment on Mild steel Plate

Similarly the experiment was conducted by selecting various parameter levels.

Regression Analysis for Mild Steel:

The regression equation is

$$\text{EXP MRR} = -405 + 2.52 \text{ Pressure} + 1.23 \text{ Cutting Speed} + 0.160 \text{ AFR} \text{---- (2)}$$

Experiment on EN8 Plate

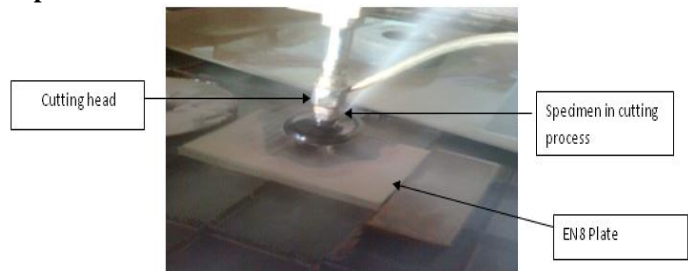


Figure 6 Experiment on EN8 plate

Similarly the experiment was conducted by selecting various parameters levels.

Regression Analysis for EN8 plate

The regression equation is

$$\text{EXP MRR} = -711 + 4.74 \text{ Pressure} + 0.415 \text{ Cutting speed} + 0.395 \text{ AFR} \text{----(3)}$$

Analysis and discussions

Three Regression equations are given below. eq (1),(2),(3).

$$\text{Aluminum MRR} = -2326 + 16.1 \text{ Pressure} + 0.757 \text{ Cutting speed} + 0.959 \text{ AFR}$$

$$\text{Mild steel MRR} = -405 + 2.52 \text{ Pressure} + 1.23 \text{ Cutting speed} + 0.160 \text{ AFR}$$

$$\text{EN8 MRR} = -711 + 4.74 \text{ Pressure} + 0.415 \text{ Cutting speed} + 0.395 \text{ AFR}$$

Validation

Validity of this above model was tested by following method.

1. Statistical indicators
2. Experimental validation

1 Statistical Indicators

a) F test - F test of all three materials indicates that model significantly represents the actual process.

b) Coefficient of determination  $R^2$ - Examination of  $R^2$  calculated for all three materials indicates that predictors explain 99% of the variance in material removal rate for Aluminum.

Similarly 88.5% for Mild Steel plate.

Similarly 96.1% for EN8 plate.

c) P-value- P value in Analysis of variance table shows 0.000. Value indicates that equation estimated by regression process is significant at  $\alpha = 0.05$

2) Experimental Validation

a) Experimental validation was carried out using validation test run and % of error between predicted material removal rate and experimental material removal rate as shown in table- 7,11,15. This test run also indicates model significantly explain the relationship between material removal rate and independent variables.

Comparison of Three Materials

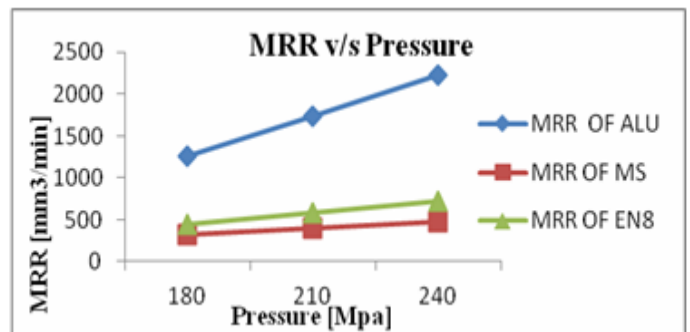


Figure 7. MRR versus Pressure at Maximum Cutting Speed

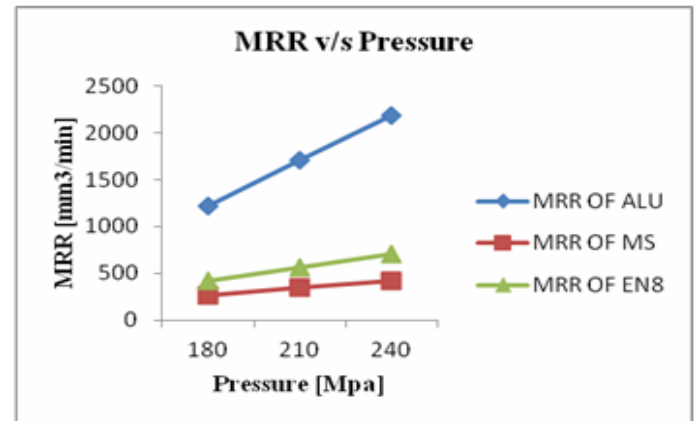


Figure 8. MRR versus Pressure at Minimum Cutting Speed

Comments on Effect of Pressure on MRR

The graphical interpretation in figure 7 and 8 shows that as the pressure increases the MRR increases. This is due to fact that as the pressure increases; velocity of jet stream of water also increases. The potential energy of the jet stream is converted in to kinetic energy and increase in the velocity of the stream of water consequently increases the metal removal rate.

It is observed that rate of increased of MRR is higher in aluminum as compared to EN8 and Mild Steel. The reason behind this is the hardness of material. Hardness is resistance to abrasion or resistance to cutting. Hardness of aluminum, Mild steel and EN8 are 95, 120, 152 BHN resp. Therefore rate of increase of MRR is higher in Aluminum. In spite of higher hardness of EN8 compared to M.S; higher MRR for EN8 is seen. This is due to fact presence of manganese and sulfur in EN8, which increases the machinability, which enhances the material removal rate.

Table 7. Comparison of Experimental MRR V/S Predicted MRR

Sr. No	Pressure	Cutting Speed	AFR	Avg Kerf	Avg. DOC	Exp MRR	Predicted MRR	% Error
	Mpa	mm/min	gm/min	Mm	mm	mm <sup>3</sup> / min	mm <sup>3</sup> / min	
1	180	125	600	0.925	11.0449	1277.067	1241.15	2.812427
2	180	125	300	0.86	9.6951	1042.233	953.45	8.517681
3	210	125	600	0.9125	15.1777	1731.206	1724.15	0.407601
4	210	125	300	0.89	12.9894	1445.071	1436.45	0.596562
5	240	125	600	0.9375	18.8129	2204.637	2207.15	-0.114
6	240	125	300	0.87	17.1056	1860.234	1919.45	-3.18326
							Avg Error	1.506168

Table 8. Experimental MRR in Mild Steel Plate

Sr No	Pressure	Cutting Speed	AFR	Average Kerf	Average DOC	Exp. MRR
	Mpa	mm/min	gm/min	mm	mm	mm <sup>3</sup> /min
1	180	170	600	0.6525	2.8842	319.929
2	180	170	300	0.635	2.7765	298.543
3	180	110	600	0.6525	4.5377	325.693
4	180	110	300	0.6325	3.7558	262.342
5	210	170	600	0.6575	3.7916	423.806
6	210	170	300	0.64	3.3407	362.048
7	210	110	600	0.6575	4.4744	323.610
8	210	110	300	0.6375	4.2943	302.318
9	240	170	600	0.645	5.01	549.3465
10	240	170	300	0.6375	4.45	482.268
11	240	110	600	0.6575	5.7688	415.642
12	240	110	300	0.6375	5.1813	363.338

Table 9. Estimated Regression coefficient for MRR

Sr.No	Predictor	Coef	SE Coef	T	P
1	Constant	-404.53	99.14	-4.08	0.004
2	Pressure	2.5198	0.3945	6.39	0.000
3	Cutting Speed	1.2324	0.3221	2.48	0.038
4	A F R	0.15991	0.06441	3.83	0.005

S = 33.4705      R-Sq = 88.5%      R-Sq(adj) = 84.2%

Table 10. Analysis of Variance for MRR

Sr.No	Source	DF	SS	MS	F	P
1	Regression	3	69024	23008	20.54	0.000
2	Residual Error	8	8962	1120	---	---
3	Total	11	77987	---	---	---

Table 11. Comparison of Experimental MRR v/s Predicted MRR in Mild Steel

Sr No	Pressure	Cutting speed	AFR	Avg Kerf	Avg Doc	Exp MRR	Predicted MRR	%Error
	Mpa	mm/min	gm/min	Mm	mm	mm <sup>3</sup> / min	mm <sup>3</sup> / min	
1	180	140	600	0.6575	4.0577	373.5113	316.8	-4.36
2	180	140	300	0.6425	2.87444	258.5523	268.8	-3.96
3	210	140	600	0.6575	4.61631	424.9313	392.4	7.65
4	210	140	300	0.6375	3.7631	335.8567	344.4	-2.54
5	240	140	600	0.6575	5.8148	535.2523	468	9.72
6	240	140	300	0.6475	4.3845	394.3858	420	-6.49
							Average Error	0.0027

Table 12. Experiment No -1 Calculated Data for Regression Equation

Sr. No.	Pressure	Cutting Speed	AFR	Average kerf	Average doc	Exp MRR
	Mpa	mm/min	gm/min	mm	mm	mm <sup>3</sup> /min
1	180	110	600	0.7475	5.2323	430.2259
2	180	110	300	0.7125	4.1089	322.035
3	180	60	600	0.7525	8.36	377.454
4	180	60	300	0.72	7.4177	320.4446
5	210	110	600	0.75	6.9236	571.197
6	210	110	300	0.7175	5.1436	405.9586
7	210	60	600	0.7525	11.4629	517.5499
8	210	60	300	0.7225	9.9737	432.3599
9	240	110	600	0.755	9.1072	756.353
10	240	110	300	0.725	7.0074	558.8402
11	240	60	600	0.755	15.13	685.389
12	240	60	300	0.725	13.49	586.815

**Table 13. Estimated Regression coefficient for MRR**

Sr.No	Predictor	Coef	SE Coef	T	P
1	Constant	-711.26	91.23	-7.80	0.000
2	Pressure	4.7385	0.3820	12.40	0.000
3	Cutting Speed	0.4153	0.3743	1.11	0.299
4	A F R	0.39540	0.06238	6.34	0.000

**Table 14. Analysis of Variance (ANOVA) for MRR**

Sr.No.	Source	DF	SS	MS	F	P
1	Regression	3	205169	68390	65.09	0.000
2	Residual Error	8	8405	1051	---	---
3	Total	11	213574	---	---	---

**Table 15. Experiment No-2 Calculated Data for Validation Test:**

Sr No	Pressure Mpa	Cutting Speed mm/ min	AFR gm/ min	Avg. Kerf mm	Average DOC mm	Exp. MRR mm <sup>3</sup> / min	Predicted MRR mm <sup>3</sup> / min	% Error
1	180	85	600	0.7525	6.0215	385.1502	414.475	-7.61386
2	180	85	300	0.715	5.204	316.2731	295.975	6.417903
3	210	85	600	0.7525	8.7953	562.5694	556.675	1.04776
4	210	85	300	0.715	6.9013	419.4265	438.175	-4.47003
	240	85	600	0.755	11.2417	721.4361	698.875	3.127248
6	240	85	300	0.725	9.3213	574.4251	580.375	-1.0358
							Average Error	0.42113

**Table 16. MRR Calculated for Three Materials Parameters using Regression Equation**

Sr.No.	Pressure Mpa	Cutting Speed mm/min	AFR gm/min	MRR of ALU mm <sup>3</sup> /min	MRR of MS mm <sup>3</sup> /min	MRR of EN8 mm <sup>3</sup> /min
1	180	150	600	1260.95	329.1	441.45
2	180	150	300	973.25	281.1	322.95
3	180	125	600	1242.025	298.35	431.075
4	180	125	300	954.325	250.35	312.575
5	180	100	600	1223.1	267.6	420.7
6	180	100	300	935.4	219.6	302.2
7	210	150	600	1743.95	404.7	583.65
8	210	150	300	1456.25	356.7	465.15
9	210	125	600	1725.025	373.95	573.275
10	210	125	300	1437.325	325.95	454.775
11	210	100	600	1706.1	343.2	562.9
12	210	100	300	1418.4	295.2	444.4
13	240	150	600	2226.95	480.3	725.85
14	240	150	300	1939.25	432.3	607.35
15	240	125	600	2208.025	449.55	715.475
16	240	125	300	1920.325	401.55	596.975
17	240	100	600	2189.1	418.8	705.1
18	240	100	300	1901.4	370.8	586.6

**Table 17. Effect of Pressure on MRR (At Maximum Cutting Speed)**

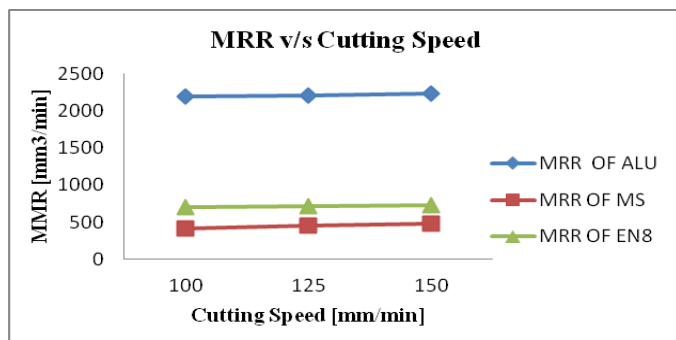
Sr. No.	Pressure Mpa	Cutting Speed mm/min	AFR gm/min	MRR of ALU mm <sup>3</sup> /min	MRR of MS mm <sup>3</sup> /min	MRR of EN8 mm <sup>3</sup> /min
1	180	150	600	1260.95	329.1	441.45
2	210	150	600	1743.95	404.7	583.65
3	240	150	600	2226.95	480.3	725.85

**Table 18. Effect of Pressure on MRR (At Minimum Cutting Speed)**

Sr. No.	Pressure Mpa	Cutting Speed mm/min	AFR gm/min	MRR of ALU mm <sup>3</sup> /min	MRR of MS mm <sup>3</sup> /min	MRR of EN8 mm <sup>3</sup> /min
1	180	100	600	1223.1	267.6	420.7
2	210	100	600	1706.1	343.2	562.9
3	240	100	600	2189.1	418.8	705.1

**Table 19. Effect of Cutting Speed on MRR (At Maximum Pressure)**

Sr. No.	Pressure Mpa	Cutting Speed mm/min	AFR gm/min	MRR of ALU mm <sup>3</sup> /min	MRR of MS mm <sup>3</sup> /min	MRR of EN8 mm <sup>3</sup> /min
1	240	100	600	2189.1	418.8	705.1
2	240	125	600	2208.025	449.55	715.475
3	240	150	600	2226.95	480.3	725.85



**Figure 9 MRR versus Cutting Speed at Maximum Pressure**  
**Comments on Effect of Cutting Speed on MRR**

The trend in the cutting speed figure 9 shows that the MRR in all three materials marginally increases as the cutting speed increases. This shows that there is no impact of cutting speed on material removal rate (MRR).

This happens due to following reason; MRR is product of DOC, width of kerf, and cutting speed. When cutting speed increases time for penetration reduces, as a result depth of cut decreases, the product of DOC, cutting speed remains constant hence MRR remains unaffected. It indicates that cutting speed is not a significant parameter to MRR. This is also reflected in p-value in regression analysis tables.

#### Discussions:

- There are number of phenomenon associated with AWJ cutting such as particles interference and fragmentation.
- The water pressure and abrasive flow rate is associated with an increase in the depth of cut. Abrasive particle available in jet which make effective impact on the work material automatically enhance the MRR.

#### Conclusions

- The parameters effective to MRR were identified using ANOVA technique. Assumptions of ANOVA were tested using residual analysis. After careful testing results show that pressure and abrasive flow rate parameters are most significant factor.
- While cutting speed are non-significant factor to MRR in AWJM. Machining of all the material with AWJM is accomplished by solid erosion. This means that increasing the pressure the abrasive grains or particles will have high speed and high energy which result good material removal rate

- The maximum prediction error for Aluminum plate in 8.5% and average error of prediction in 1.506, Mild Steel plate maximum error of prediction 9.72% and average error of prediction is .0027 and EN8 Plate maximum error of prediction is 7.61% and average error of prediction is 0.42.

#### Future Scope

- Present study shows effect of three main operating parameters on material removal rate. This can be further extended to include remaining machine parameters such as standoff distance, abrasive size and focusing tube diameter/length to get deeper understanding of process.

#### Acknowledgement

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