



## Mechanical Engineering

Elixir Mech. Engg. 70 (2014) 24032-24035

Elixir  
ISSN: 2229-712X

# A Review on Cohesive Zone Modeling For Analysis of Crack Propagation in Adhesive Joints

M.D.Mohan Gift<sup>1\*</sup>, P.Selvakumar<sup>2</sup> and S.John Alexis<sup>3</sup>

<sup>1</sup>Department of Mechanical, Panimalar Engineering College, Chennai.

<sup>2</sup>Department of Mechanical, Paavai Engineering College, Salem.

<sup>3</sup>Department of Indus Engineering College, Coimbatore.

### ARTICLE INFO

#### Article history:

Received: 19 November 2013;

Received in revised form:

25 April 2014;

Accepted: 5 May 2014;

#### Keywords

Cohesive zone model,  
Finite Element Analysis,  
Virtual Crack Closure Technique,  
Single Lap Joint,  
Double Cantilever Beam,  
Strain Energy Release Rate,  
Back Face Strain.

### ABSTRACT

Adhesive joints are used in a wide range of industrial applications due to their advantages over other joints. The crack propagation analysis in an adhesive joint is very important for its sustained performance. The Cohesive zone model (CZM) is found to be effective in this area due to its advantage over traditional methods. An overview of the CZM, usage with Finite Element Analysis (FEA), comparison with other methods, and implementation by back face strain (BFS) technique are reviewed in a proportional manner

© 2014 Elixir All rights reserved

### Introduction

Adhesive bonding of metallic plates is an effective joining method in many industrial applications. Adhesive bonding is a material joining process in which an adhesive, placed between the surfaces, solidifies to produce an adhesive bond. Adhesively bonded joints are increasing alternatives to mechanical joints in engineering applications. They provide many advantages over conventional mechanical joints. Adhesive joints provide galvanic isolation, vibration damping, sealing capacity, high corrosion and fatigue resistance, and crack retardation. Also adhesive joints are used to join complex shapes and reduce the weight of structures. The cohesive zone model (CZM) is an approach which is used extensively in the analysis of crack propagation in adhesive joints.

#### Cohesive zone model (CZM):

The CZM was introduced by Barenblatt[1] which is based on the Griffith's theory of fracture. The CZM was used to describe the crack propagation in perfectly brittle materials by assuming that finite molecular cohesion forces exist near the crack face. Then, Dugdale [2] modified the approach by considering the existence of a process zone at the crack tip and extended it to perfectly plastic materials. It was suggested in this approach that the cohesive stresses in the CZM are constant and equal to the yield stress of material. Because of its flexibility, cohesive zone models are increasingly used in many engineering fields like crack tip plasticity, creep under static and fatigue loading, adhesive bonded joints, crack bridging, and interface cracks in bimetals.

#### Need of CZM for fracture analysis of adhesive joints:

CZMs are used for accurate predictions of the adhesive joint strengths, deformations, interface failure, and the change between adhesive failure and the adherend failure which is not possible with conventional fracture mechanics. Because of the

presence of increased plasticity in the adherends during deformation, the traditional approaches are not effective for analyzing the fracture of adhesive joints. CZMs use an approach which allows flexibility during adhesive deformation. The following reviews establish the need of the CZM for the fracture analysis of adhesive joints when compared to regular fracture mechanics approaches.

T.Ferracin et al[3] suggests the problems involved in the usage of existing analytical non-linear fracture mechanics models for fracture analysis of adhesive joints when the amount of plasticity within the adhesive bond is extensive. Also the difficulty exists when an attempt is made to characterize the cracking resistance of adhesive bonds experimentally. Development of mechanical tests from which important adhesive fracture properties can be analysed is also complicated. F.Ascione et al[4] used a CZM which used two approaches for the stress and deformation of the adhesive joints. The CZMs were found to be effective as it considered all the factors important for the adhesive joint behavior namely, adherend and adhesive properties, joint geometry, total length, etc.

S.Li et al[5] in his work suggests that the strength of adhesive joints have been evaluated by two approaches namely strength based criteria and energy based criteria. CZMs strive to combine these two approaches which is a good advantage. Especially when the adherends are subjected to plastic deformation, cohesive models are used for analysis which is not possible by regular methods. CZMs are found to predict quantitatively, the mode-I fracture of adhesively bonded joints. S.Marzi et al[6] suggests that a major problem in the regular methods is the assumption of the existence of a crack for its implementation which is solved using a cohesive model. This is done by modeling the adhesive layer as a cohesive surface with properties given by the cohesive law

Tele:

E-mail addresses: [mdgift@gmail.com](mailto:mdgift@gmail.com)

© 2014 Elixir All rights reserved

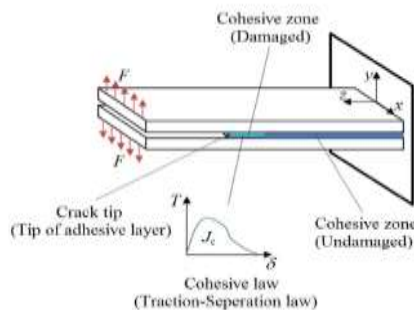
The CZMs provide an alternative solution when the regular methods used for crack prediction like virtual crack closure technique (VCCT), and the J integral are not effective. This is because these methods need geometrical information about the crack profile that is needed for finding the energy release rate ( $G$ ) as suggested by C.Fan et al[7]

Thus we can clearly understand that the CZMs can be used effectively in analyzing the crack propagation in adhesive joints when compared to the regular methods as seen by the following points.

- Regular methods need accurate geometrical information about the crack profile.
- Assumption of the existence of a crack is needed for implementation of the methods.
- Regular methods are inaccurate when plasticity in the adhesive joints is large

#### Overview of the CZM application in the crack propagation study in adhesive joints:

The procedure for applying the CZM to analyse crack propagation in adhesive joints generally involves a cohesive zone. This zone is considered as two cohesive surfaces which are attached by a cohesive traction. The failure is approximated by the complete separation of the two surfaces. This is explained with the help of a cohesive law which relates the cohesive traction and separation of the surfaces.



At the starting point of the crack, a damage zone is formed. Based on the beginning of damage, a stress limit is set based on the material strength. When the stress limit is attained, the damage starts. After this, due to the increase of the relative displacement between the two cohesive surfaces, the stress begins to decrease. Finally, the stress is reduced to zero resulting in a new area of crack as outlined by C.Fan et al[7]

In analysis of crack propagation in adhesive joints, a predefined crack path needs to be defined. Along this path, the CZM specifies a traction-separation law which is a relation between coincident surfaces on either side. As the separation increases, the traction across the interface reaches a maximum limit and decreases. The crack finally propagates resulting in a total detachment of the surfaces as suggested by MD Banea et al [8].

#### Usage of CZM with FEA in the analysis of crack propagation in adhesive joints:

The use of cohesive zone models (CZM's) with FEA is the most prevalent method of predicting crack propagation in adhesive joints. Within finite element calculations, the CZM is used to analyse both the fatigue and failure loads of adhesive joints. Both cohesive strength and toughness are used to describe the failure behavior of adhesive joints in the implementation of CZM with FEA.

A simple model with an assumption that the adherends are in tension and the adhesive is in shear and both the stresses do not vary across the thickness was given by Volkerson[19] for the analysis of Crack propagation in adhesive joints. The effects

of the peel stress and shear stress and also bending of the adherend were taken into account by Goland and Reissner[20].

The finite element method was more superior to the finite difference method as it can adopt any geometric shape under loading and also the numerical simulation. FEA has the ability to consider the stress variation throughout the thickness of the adhesive joint. The material and geometrical non-linearity can be included in the analysis. H.Kim and K.Edward[21] used the finite difference method to analyse the adhesive joints. The finite element method was used by Penado and Dropek[22] for adhesive joint analysis.

The CZM with FEA is used to replicate the adhesive failure by using two approaches namely the Adherent Cohesive zone and the Adherent Adhesive Cohesive zone. The first approach considers the adherents and the adhesive layer which is considered as a cohesive zone where the traction-separation replicates the behavior of the adhesive. The second approach has a finite thickness layer in addition to the adhesive layer. This has an advantage for more accuracy in simulation of adhesive behavior as suggested by Imanaka et al[23]

A non-linear finite element method was used for failure mode and load prediction by Harris and Adams[24]. Single lap joints with Aluminium adherends were used for the analysis. The finite element method established the need for different criteria for different adhesive systems. A.Ozel et al[25] also used non-linear FEM for analyzing crack propagation in a SLJ. For this analysis, two adhesives having varying mechanical behavior were used. The adherend was hard steel having four different thicknesses. Comparison between the FEA results and the experimental work were found to coincide to a certain level

Jie Feng et al[26] used a CZM based finite element model to verify the fracture behavior of a rubber toughened epoxy. The fracture behavior was dependent on thickness and also related to the plastic zone developed in the adhesive layer which was confirmed by FEA.

Andruet et al[27] used both two and three dimensional elements which was developed for displacement and stress analysis in adhesively bonded joints. The analysis was done on a single lap joint in which both two and three dimensional stress analysis was done.

Ljungqvist[28] used spring elements in a FEM used for simulating the adhesive behavior in adhesive joints. Different methods which replicated the adhesive behavior were done in the analysis.

M.M.Abdel Wahab et al[29] used a Finite Element procedure which was used to predict the fatigue behavior of an adhesively bonded composite joint. The procedure involved an experiment consisting of a DCB specimen which was used to determine a crack growth law. The law was further implemented within a finite element method which was used to generate the load-life response of joints having different configurations.

H.Khoromishad et al[30] developed a Finite Element method which was used to predict the static response of a Single lap adhesive joint. The model was developed in ABAQUS where four noded plane stress elements were used for the substrates and four noded Cohesive elements were used to analyse the adhesive bond-line.

The CZM coupled with FEA was used for a comparative study of strain distribution in adhesively bonded joints by Colavito et al[31]. The FEA results were validated by experiments done using Digital Image Correlation(DIC).

S.Yang et al[32] used a FEM in ABAQUS which successfully simulated composite adhesive joints with delaminations and cracks between the adherend and the adhesive.

P.Raos et al[33] implemented both 2D and 3D methodologies in FEM to analyse fatigue behavior in SLJs. The variations were adopted for overlap length and the physical characteristics of the adhesive and the adherend.

The usage of CZM and FEA involving modeling of both the adhesive and the adherends using shell elements was done by Naboulsi and Mall[34]. The modeling met the requirement related to the bending properties of the adhesive joints as it was found to give reasonable results.

The CZM application with FEM was done by modeling the adhesive as an elastoplastic continuum using solid FE elements by Pardoen et al[35].

#### **Comparison of CZM with Virtual Crack Closure Technique (VCCT) in the analysis of crack propagation in adhesive joints**

The VCCT is a methodology which is used for calculating the Strain Energy Release Rate (SERR) in the analysis of crack propagation in adhesive joints. Several literatures are reviewed in the process of comparison of VCCT and CZM to validate the effectiveness of CZM in crack propagation analysis.

The CZM is considered for modeling both crack initiation and propagation which has an edge over the VCCT in the analysis of crack propagation in adhesive joints according to the works of Rybicki E F[36] and Wood MDK [37].

Ye Zhang et al[38] compared the VCCT and CZM in an experimental study of an Adhesive joint involving Double Cantilever Beam (DCB) specimens of Glass Fiber-Reinforced Polymer (GFRP) laminates. The outcome established the validity of both the methods and outlined the advantages of each technique. The CZM allowed accommodating ductile fracture behavior to be modeled and also gave results which were coincident with the experimental data.

Ruixiang Bai et al[39] obtained the values of SERR using both the VCCT and the CZM in an analysis of an adhesive joint involving piezo-electric composites. The CZM provided a superior degree of coincidence in the load-displacement reaction when compared with VCCT. The VCCT was not able to simulate the crack initiation phase like the CZM.

When compared with VCCT, the CZM is able to calculate the commencement and spread of a crack without the need to apply a pre-existing crack

#### **The usage of back-face strain technique in the framework of the CZM:**

The Back-face strain (BFS) values are basically used to validate the results obtained in the analysis of crack initiation and propagation in an adhesive joint using the CZM. BFS technique was basically developed to detect the crack initiation in adhesive joints. Initially, the BFS technique was employed by Abe and Satoh [40] in the analysis of crack initiation and propagation of welded joints.

The crack initiation in an adhesive joint can be assessed by noticing the change in the direction of the back-face strain as proved in the work of Zhang et al[41]. Furthermore, Crocombe et al[42] was able to establish that the crack initiation in the adhesive joint was detected based on the response of the BFS location. Khoromishad et al[43] was able to extend the BFS technique for the crack initiation along with the propagation in single lap adhesive joints.

Graner Solana et al [44] developed an elasto-plastic damage model which predicted the backface strain observed from experiments and fatigue life at different fatigue loads. An

experiment was conducted in which six strain gauges were placed along the overlap in a Single Lap adhesive joint which monitored the crack initiation and propagation inside the adhesive layer.

#### **Conclusions**

The role of a CZM in the crack propagation analysis of an adhesive joint was explored by considering the advantages over other methods which have their limitations. This was made clear by comparing the CZM with the VCCT in the calculation of the SERR. The CZM together with FEA provided results which coincided with the experimental data. The procedure for applying the CZM for crack propagation in the adhesive joints was reviewed in a detailed manner. Finally the BFS technique in the framework of the CZM for studying the crack initiation phase in the adhesive joints was reviewed.

#### **References**

- [1] Barenblatt GI. The mathematical theory of equilibrium cracks in brittle fracture. *Applied Mechanics* 1962;7:55–129.
- [2] Dugdale DS. Yielding of steel sheets containing slits. *Journal of the Mechanics and Physics of Solids* 1960;8:100–4.
- [3] Ferracin.T , Landis.C.M , Delannay.F, Pardoen.T. On the determination of the cohesive zone properties of an adhesive layer from the analysis of the wedge-peel test *International Journal of Solids and Structures* 40 (2003) 2889–2904.
- [4] Francesco Ascione Mechanical behaviour of FRP adhesive joints: A theoretical model *Composites: Part B* 40 (2009) 116–124
- [5]. Li S, Thouless MD, Waas AM, Schroeder JA, Zavattieri PD. Mixed-mode cohesive-zone models for fracture of an adhesively bonded polymer–matrix composite. *Engineering Fracture Mechanics* 73 (2006) 64–78
- [6] Stephan Marzi, Anders Biel , Ulf Stigh On experimental methods to investigate the effect of layer thickness on the fracture behavior of adhesively bonded joints *International Journal of Adhesion & Adhesives* 31 (2011) 840–850
- [7] Chengye Fan, Ben Jar P.Y, Roger Cheng J.J Cohesive zone with continuum damage properties for simulation of delamination development in fibre composites and failure of adhesive joints, *Engineering Fracture Mechanics* 75 (2008) 3866–3880
- [8] Banea MD, Da Silva L F M Adhesively bonded joints in composite materials: an Overview *Proc. IMechE Vol. 223 Part L: J. Materials: Design and Applications*
- [9] Kafkalidis, M.S., Thouless, M.D. The effects of geometry and material properties on the fracture of single lap-shear joints. *International Journal of Solids and Structures* 39 (2002), 4367–4383.
- [10] R.D.S.G. Campilho , M.F.S.F. de Moura , J.J.M.S. Domingues Using a cohesive damage model to predict the tensile behaviour of CFRP single-strap repairs *International Journal of Solids and Structures* 45 (2008) 1497–1512.
- [11] M.F.S.F. de Moura, J.A.G. Chousal Cohesive and continuum damage models applied to fracture characterization of bonded joints *International Journal of Mechanical Sciences* 48 (2006) 493–503
- [12] Young Tae Kim MinJung Lee, ByungChai Lee Simulation of adhesive joints using the superimposed finite element method and a cohesive zone model *International Journal of Adhesion & Adhesives* 31 (2011) 357–362
- [13] Zhenyu Ouyang , Guoqiang Li , Cohesive zone model based analytical solutions for adhesively bonded pipe joints under torsional loading *International Journal of Solids and Structures* 46 (2009) 1205–1217.

- [14] Min JungLee , TaeMinCho, WonSeockKim, ByungChaiLee, JungJuLee Determination of cohesive parameters for a mixed-mode cohesive zone model *International Journal of Adhesion & Adhesives* 30 (2010) 322–328.
- [15] Liljedahl, C.D.M. et al., *International Journal of Adhesion & Adhesives* 27, 505–518, 2007.
- [16] A.Pirondi, G.Nicoletto Fatigue crack growth in bonded DCB specimens *Engineering Fracture Mechanics* Volume 71, Issues 4–6, March–April 2004, Pages 859–871
- [17] Todd W. Bjerke, John Lambros; “Theoretical development and experimental validation of a thermally dissipative cohesive zone model for dynamic fracture of amorphous polymers” *Journal of the Mechanics and Physics of Solids* 51 (2003) 1147 – 1170
- [18] Peter Feraren, Henrik Myhre Jensen “Cohesive zone modelling of interface fracture near flaws in adhesive joints” *Engineering Fracture Mechanics* 71 (2004) 2125–2142.
- [19] Volkersen, O., Die Niekraftverteilung in Zugbeanspruchten mit Konstanten Laschenquerschnitten. *Luftfahrtforschung* 15, 1938, pp. 41-47.
- [20] M. Goland and E. Reissner, “The Stresses in Cemented Joints,” *Journal of Applied Mechanics* 11, 1944, pp. A17-A27
- [21] H. Kim and K. Kedward, “Stress Analysis of Adhesively-Bonded Joints Under In-Plane Shear Loading,” *J. Adhesion*, Vol. 76, 2001, pp.1-36.
- [22] F.E. Penado and R.K. Dropek, “Numerical Design and Analysis,” *Engineered Materials Handbook*, Volume 3 “Adhesives & Sealants”, ASM International, 1990.
- [23] Imanaka, M., Nakamura, Y., Nishimura, A., Iida, T. Fracture toughness of rubber-modified epoxy adhesives: effect of plastic deformability of the matrix phase, *Composites Science and Technology*, (2003), 63(1), Pages 41-51
- [24] J.A. Harris and R.D. Adams, “Strength Prediction of Bonded Single Lap Joints by Nonlinear Finite Element Methods,” *International Journal of Adhesion and Adhesives*, Volume 4, Issue 2, pp. 65-78, April 1984.
- [25] A. Ozel, F. Kadioglu, S. Sen & R. Sadeler “Finite element analysis of adhesive joints in four-point bending load” *The Journal of Adhesion* Volume 79, pages 683-697 Issue 7, 2003.
- [26] Jie Feng, Hua Liu and Gavin Vogel “Analysis of Adhesive Geometric Effect on Fracture Behavior in Applying Rubber Filled Epoxy Materials” adhesives, epoxy, markets, polymers, Antec 2011 1 May 2011
- [27] R.H. Andruet, D.A. Dillard and S.M. Holzer, Two and three-dimensional geometrical nonlinear finite elements for analysis of adhesive joints, *International Journal of Adhesion & Adhesives* 21 (2001), pp. 17-34.
- [28] H. Ljungquist, Constitutive Modelling of Adhesive Joints and Application to Impact Analysis for a Truck Cab Using the Finite Element Method, Division of Solid Mechanics, Chalmers University of Technology (1997).
- [29] M.M. Abdel Wahab, I.A. Ashcroft, A.D. Crocombe, P.A. Smith “Finite element prediction of fatigue crack propagation lifetime in composite bonded joints” *Composites: Part A* 35 (2004) 213–222
- [30] H. Khoramishad , A.D. Crocombe , K.B. Katnam , I.A. Ashcroft “Fatigue damage modelling of adhesively bonded joints under variable amplitude loading using a cohesive zone model” *Engineering Fracture Mechanics* 78 (2011) 3212–3225.
- [31] Colavito KW, Gorman J, Madenci E. Refinements in digital image correlation technique to extract adhesive strains in lap joints. 50th AIAA/ASME/ASCE/ AHS/ASC Structures, structural dynamics, and materials conference, Palm Springs: California; 4–7 May 2009
- [32] Shuo Yang , Lan Gu, Ronald F. Gibson “Nondestructive detection of weak joints in adhesively bonded composite structures” *Composite Structures* 51 (2001) 63±71
- [33] P. Raos, M. Lucić, F. Matejiček. “Experimental and Numerical Analysis of Lap Length Influence on Strength of Adhesively Bonded Joint” in *Proceedings of PPS-18* (CD-Book), Guimarães, Portugal. 2002.
- [34] Naboulsi S, Mall S. Thermal effects on adhesively bonded composite repair of cracked aluminum panels. *Applied Fracture Mechanics* 1997
- [35] T. Pardoan, T. Ferracin, C.M. Landis, F. Delannay, Constraint effects in adhesive joint fracture. *J. Mech. Phys. Solids* 53, 1951–1983 (2005)
- [36] Rybicki EF, Kanninen MF. A finite element calculation of stress intensity factors by a modified crack closure integral. *Engineering Fracture Mechanics* 1977; 9(4): 931-938.
- [37] Wood MDK, Sun X, Tong L, Katzos A, Rispler A, Mai Y. The effect of stitch distribution on Mode I delamination toughness of stitched laminated composites – experimental results and FEA simulation. *Composites Science Technology* 2007; 67(6): 1058-1072.
- [38] Zhang.Y, Vassilopolous.A.P, Keller.T, “Mode I and II fracture behavior of adhesively-bonded pultruded composite joints”, *Engineering Fracture Mechanics*, Vol. 77, Issue 1, 2010, pp. 128-143
- [39] Ruxiyaing Bai, Liang Wang, Zhenkun Lei, Haoran Chen, “Experimental and numerical analysis of interfacial fracture in piezoelectric composite” *OptoElectronics and Advanced Materials – Rapid Communications* Vol. 5, No. 12, December 2011, p. 1328 – 1335
- [40] Abe H, Satoh T. Non-destructive detection method of fatigue crack in spot-welded joints. *Yosetsu Gakkai Ronbunshu/Quarterly Journal of the Japan Welding Society* 1986;4:666-73.
- [41] Z. H. Zhang, J. K. Shang, and F. V. Lawrence, “A back-face strain technique for detecting fatigue-crack initiation in adhesive joints,” *The Journal of Adhesion*, vol. 49, no. 1-2, pp. 23–36, 1995.
- [42] A. D. Crocombe, C. Y. Ong, C. M. Chan, M. M. A. Wahab, and I. A. Ashcroft, “Investigating fatigue damage evolution in adhesively bonded structures using backface strain measurement,” *The Journal of Adhesion*, vol. 78, no. 9, pp. 745–776, 2002.
- [43] H. Khoramishad, A. D. Crocombe, K. B. Katnam, and I. A. Ashcroft, “Predicting fatigue damage in adhesively bonded joints using a cohesive zone model,” *International Journal of Fatigue*, vol. 32, no. 7, pp. 1146–1158, 2010.
- [44] Graner Solana A, Crocombe AD, Wahab MMA, Ashcroft IA. Fatigue initiation in adhesively-bonded single-lap joints. *Journal of Adhesion Science and Technology* 2007;21:1343-57.