Automatic Medical Image Annotation by using Color feature

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ABSTRACT

Automatic annotation is in fact the process of classifying medical using global and local features of standard image codes (IRMA) while being extracted. This includes four technical data axes of providing image (modality), direction, anatomy, and biological system. A few number of recent researches have been conducted on the extraction of Gabor filter feature in HSV color space for automatic annotation, but until now no complete comparison has been conducted on the accuracy of the different classifications in resolution and annotation of the images based on the Gabor filter feature in HSV color space. The results from the known and famous classifiers used on the four characteristics of anatomy, direction, biological system and modality are presented in this paper, which show that K-Nearest Neighbor is the most efficient classification group as far as accuracy is concerned.

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Introduction

Automatic annotation of medical image is an emerging technology and now still is considered as an important tool for the physicians in their daily activities, which is the subject of discussion for many of the radiology physicians. And reasonable studies have been conducted in this context. Nowadays hospitals create a huge amount of the data, which is the calculated by the size of the radiological groups producing multiple tera-bytes of data year.

Apart from this, the manual annotation causes errors in the labels, such that part of the available knowledge is no more accessible to physicians, Guleld et al in 2002. [1].This calls for individuals requirements to be able to develop proper algorithms to automatically annotate the medical images. [2]. image annotation could be done in a manual, semi-automatic and automatic method. In the manual method of annotation, human power is used. The accuracy of this kind of annotation is high, but it is a boring process in the long run, and the users mostly ask to use other alternative methods. [3]. Content based image retrieval (CBIR) systems distinguish images based on their visual feature such as color, texture, and shape.[4] but mostly among the content features of lower level (color- texture-shape) and high level meaningful features used by humans, for description Of the image, there is a semantic gap. [5]. To map bridge the semantic gap, the automatic annotation is used. In the automatic annotation method, we try to produce annotation through machines; the accuracy of this method is lower than the other methods. In this method, the classification of images is totally based on features extracted by using image processing techniques and machine learning algorithms and the use of training data is done. [5].In the semi-automated method, the user's participation is required for the image annotation process. With regard to the quality of human modification, compared with manually annotated, this process has improved. [3].

Tian et al in [6], proposed combining extracted features, local binary pattern methods and MPEG-7, and SVM Classifier for automatic annotation of medical images. The best method results presented in this paper was obtained by using the 330 elements extracted feature vector. Thomas et al [7], in another system, proposed a combination of local binary pattern features [8] and produced SIFT and SVM Classifier. The method presented in this paper had the best results in the Image CLEF2008. Dmitrovski et al [9], developed a hierarchical system for multi-label annotation of medical images. They have used different methods of feature extraction & combination and combinational classifiers of bagging and random forests.

Vailaya et al [10], used non-parametric Bayesian approach for classifying the images. Instead of segmenting, they directly cluster and calculate the image features for conditional probabilities. Dzeroski et al [11], used a combination of machine learning algorithms (Boosting) to annotate medical images. This method is based on the combined results of the weak classifiers to generate strong classifiers with very high accuracy. The purpose of this method is to combine several classifiers with less precision in order to make a highly accurate classifier.

The proposed method of this paper is based on two steps of annotation, i.e., feature extraction and classification of images. For the feature extraction part, Gabor filter feature in HSV color space, which is one of the most powerful and most used color features, is used; and for the classified images part, the images are classified using various machine learning algorithms. In this paper conclusions employing Gabor filter feature in HSV color space of various classifiers on the four classes (modality- direction- anatomy- biological system) are investigated.

Section 2 describes the methodology used to test the data set that is an introduction of used data set, feature extraction techniques, and evaluation of the various classifiers such as

support vector machine - Decision trees - Bayesian methods - Bagging and Boosting combination all methods, etc. The accuracy of the experimental results obtained from the application of these well-known provisions on the four characteristics (modality-direction- anatomy- biological system) is presented in Section 3. Section 4 contains the complete results of the investigation.

Testing method

This section explains the implied data set and introduces the features method extracted from the image and the reviews the different classifiers for each system data axis of annotation. The purpose of this paper is to obtain the highest accuracy in the area of classifier algorithms for automatic medical image annotation, using Gabor filter feature in HSV color space.

Data set

The Image Retrieval on Medical Application (IRMA) data set is a database to create an automatic medical image annotation system which is presented by the IRMA group from the Anchen University Hospital, Germany [12]. This set is used for calling ImageCLEF medical image annotation, and has dealt with comparing the performed work from 2005 to 2009. [13]. Image classification work was started in 2005 with 57 classes; this figure raised to 116 by 2006, but since 2007 image annotation includes a 13 character IRMA code. An ImageCLEF2007 dataset which includes a 10000 training image and 10000 test images has been used for this paper.

IRMA is a 13 character code and is used to describe a class or annotation of a medical image. The Schema of IRMA code has four axes, each of which has a three to four positions. Each position has a value of a 0 to 9, a to z set given to it, in which the amount of "0" denotes "unspecified" and determines the end of a Path along the axis. These four axes are:

1- Technical axis (T, image modality) explains the method used to obtain the image.

2- Directional axis (D, body orientation) describes the direction of photographing the body organ.

3- Anatomical axis (A, body region) indicates the body organ presented in the image.

4- Biological axis (B, biological system) describes the biological system of the organ presented in the image including cardiovascular-spinal and muscular. IRMA code can be shown as follows:
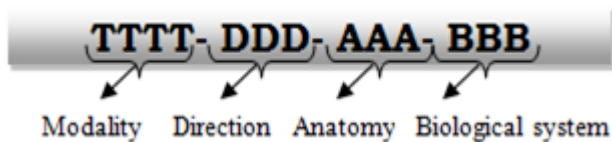

Figure 1. Schema of IRMA code [9, 2].

Examples of the annotation medical images along with the 13 character IRMA code has been shown in Figure 2.

Figure 2. Examples of annotated images of ImageCLEF2007 [14].

For our project, Matlab 2013 software is used to implement the extraction of the Gabor filter feature in HSV color space, and RapidMiner and Weka software has been used to measure the accuracy of the classified algorithms for automatic medical

image annotation in the various information axes of the image (modality, direction, anatomy, and biological system) on the extracted data**.**

Feature extraction

In the area of image classification and retrieval, Those are shown with low level features. Since the image is formed as a set of pixels, therefore the first step to understand the image would be to extract the visual features of the pixels. Providing the appropriate features helps to improve the process of the learning techniques immensely. In each image, by using various methods, the extractable features are classified into two groups, as names Global and Local. The global features are usually not sensitive to change in spatial or locality of different images. Local features are more appropriate for explaining the details of the image. For example, the histogram color chart can be used to show or explain the global color contents of the image. As a sample, an image can be interpreted in which 40% is blue, 37% yellow, etc. Therefore, the image can be shown globally based on parts; but the choice is usually for regional Segmentation. [5]. the method of feature extraction used in this research is explained here with.

Gabor Filter

One of the important and strong characteristics of feature extraction of texture Spectral is Gabor Filter. This characteristic in addition to texture feature extraction can be used in the HSV color space and color features can be extracted from it. This feature due to doing less computation for complexity in distance domain, is strong. This filter has improved localization properties in two areas of spatial and frequency and is appropriate for texture and color classification. This feature has high accuracy in image recognition and color analysis. 2D Gabor function is defined as follow: [15].

$$G(x,y) = \frac{1}{2\pi\delta_x\delta_y} \exp\left\{-\frac{1}{2}\left[\left(\frac{x}{\delta_x}\right)^2 + \left(\frac{y}{\delta_y}\right)^2\right] + j(ux+vy)\right\} \quad (1)$$

$$H(x,y,\phi,f) = \exp\left\{-\frac{1}{2}\left[\frac{x_\phi^2}{\delta_x^2} + \frac{y_\phi^2}{\delta_\phi^2}\right]\right\}\cos(2\pi f x_\phi)$$

$$x_\phi = x\cos\phi + y\sin\phi, \quad y_\phi = -x\sin\phi + y\cos\phi \quad (2)$$

φ is the direction of filter and F is the frequency. δ_x and δ_y are Gaussian envelope function along X and Y axis.

Selecting these parameters is very important in feature extraction. Image feature extraction technique (Gabor Filter), is considered as follow:

Image conversion of RGB color space to HVS color space

1) Color feature extraction in Gabor filter from each medical dataset image. (In this stage, at first, a bank of Gabor filter is created on images in different frequencies and directions. And number of filters for each image is extracted).

Gabor filter, usually, is formed in 4 frequencies and in different direction of 0 to 180 degrees. Then, the extraction of two means parameters and standard deviation will be done on each of the filtered image.

3) Creating histogram of Gabor filter feature extraction, from each image of second step.

Table 2, shows the length of feature vector from Gabor filter feature extraction.[15].
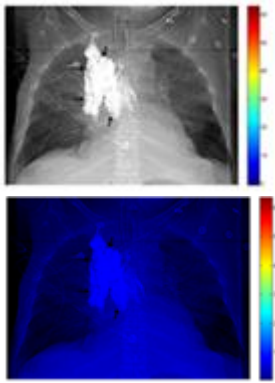
Figure 3. Shows an image sample with the histogram implementation of Color feature extraction in Gabor filter.
A) **Sample image in RGB color space**
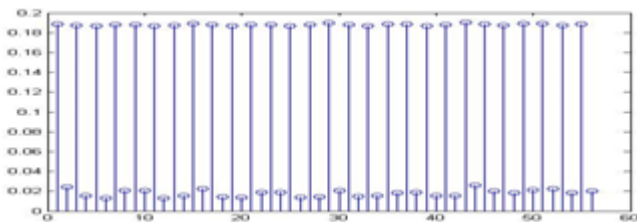B) **Sample image in HSV color space**

Figure 3. Displaying 56bins histogram from Gabor filter feature extraction with the frequency number of 4 and the direction number of 7
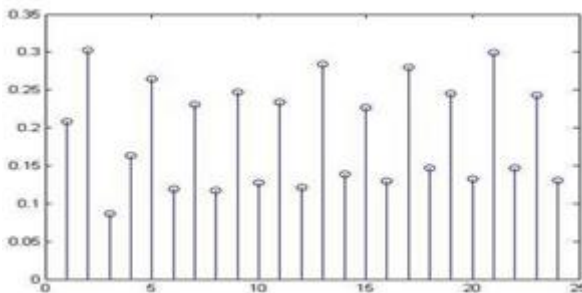

Figure 4. Displaying 26 bins histogram from Gabor filter feature extraction with the frequency number of 3 and the direction number of 4

Algorithms of medical image classification

In this section we introduce different algorithms in order to compare the accuracy of the classifiers for automatic medical annotations. They are briefly explained as follows:

Bayesian group

In the multi label annotation, an image is labeled by multi content or multi class. The meaning of multi-label method is connected with the learning discussion of multi-instance multi-label (MIML). In MIML an image is shown with a bag of features or a bag of regions. A typical MIML, using probabilistic tools, such as the Bayesian method, is achieved. The Bayesian methods work by finding the posterior probability that an image belongs to any particular concept. The Bayesian method explicitly needs all the hypotheses in the model, and it is then used optimally to extract classifier rules. The Bayesian method, with the help of training data for calculating the probability from each class with regards to special vector is made of a new sample. [5].

If a set of images $\{I1, I2, \ldots, In\}$ is taken into consideration from a set of $\{Cn, \ldots, C2, C1\}$, the Bayesian models are trying to procure posterior probability from conditional and priors probabilities. We assume that an image I, with feature vector **x** is

shown. We also have the prior probability P(Ci) and density of conditional probability P(X/Ci).

The probability that an unknown image I belongs to a Ci class is obtained from the following relation. [5].

$$P(C_i|X) = \frac{P(X|C_i)P(C_i)}{P(X)} \qquad (3)$$

- **Naive Bayes:**

This is one of the oldest official classification algorithms from the Bayesian group. This classification is a family from the probabilistic simple classifications based on using the Bayes' theorem with independent and strong hypotheses (Naive) between the features. [16].

The Naive Bayes model is known under different names such as simple Bayes and independent Bayes. All these names used from the Bayes' theorem in the decision making rules in classification. Naive Bayes has been studied widely since 1950 and was introduced with popular names in the text retrieval society from early 1960. This is a popular method (basic) for classification of texts. Naive Bayes is scalable and needs only a few linear parameters for a few variables (predications/features) in a Learning problem.

The advantage of Naive Bayes is that it needs only a few of the training data to estimate the average parameters and variances for classification.

Trees group

The decision tree is a tool of classification or a multi-level decision making. Based on some of the decisions made in each of the inner nodes, a decision tree (DT) can be a binary tree or n-ary. A decision tree classifies a sample by arranging them through a tree to an appropriate leaf node. Each node shows a number of features from the sample, and each branch is connected to some probability for this features. A number of DT algorithms are used in this literature which include j48, Decision Stump, C4.5, etc. these algorithms of DTs are different as far as the kind of feature, selection criteria, result, etc., are concerned.[5].

- **Decision stump:**

The decision stump classifier is a learning machine model comprising a one level decision tree. This means that it is a decision tree with an inner node (root) which immediately connects with the terminal nodes (leaf). The decision stump predicts with one of the input features. Sometimes it's called rules.

The decision stump classifier is often used like a basic learner or a weak learner in the complex learning machine technique such as Boosting and Bagging.

- **J48:**

J48 is another algorithm from the decision tree set, and makes a pruned or non-pruned tree from the C4.5. C4.5 tree starts from the root which shows all the data and in return divides them into smaller sets. This is done by testing each of the two groups. This process continues until all the samples are grouped together, at this time the tree stops growing.

Group support vector machine

The group support vector machine (SVM) is a supervised classifier which can learn from the samples and make decisions for the new samples. SVM can classify the data in a linear and non-linear method. In producing the SVM model in a linear manner, by finding an optimal hyperplane, the data is separated without error and maximum distance between the planes and the nearest training points (supporting vectors).

Figure 5 shows this process. All the samples have label -1 on one side of the hyperplane and all the samples have +1 label on the other side.

The training samples close to the hyperplane, is named supporting vector. The number of these supporting vectors are in comparison with the size of the training set is small and decide on the border, hyperplane and as a result the decision surface.
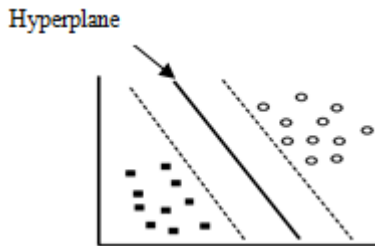

Figure 5. Production of linear SVM model [17].

In a case where the data cannot be separated in a linear manner, they are mapped in a more dimension space so that they can be separated in a linear manner in a new space.
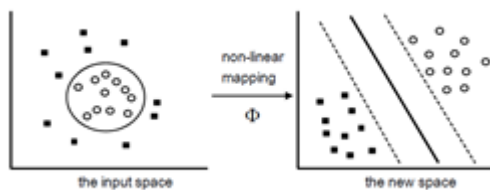

Figure 6. Production of no- linear SVM model [17].

For the implementation of SVM, with the purpose of maximizing the distance between the classes, the (SMO) version is used. The sequential minimum optimization (SMO) algorithm is a simple algorithm which can solve the Quadratic programming (QP) problems, which arise during the SVM training, quickly.

The SMO algorithm was introduced by John- Platt in 1998 in Microsoft's researches. [18]. The SMO, larger QP problems are broken into smaller possible QP problems. These small QP problems are solved analytically. The time for calculating the SMO is determined through SVM evaluation. Therefore, SMO is very fast for the linear SVM and the dispersed data set. The main idea of SMO is that after normalizing the data, the classes are mutually separated by the same method SVM.

K-Nearest Neighbor

In pattern classification, the K-Nearest Neighbor (K-NN) classifier is a conventional non-parametric classifier. To classify an unknown image displayed by some as feature vectors as a point in the feature space. The K-NN classifier, calculates the distance between points in the training data set. Then point to a class of K Nearest Neighbors (where K is an integer) is assigned for.

K-NN is an instance-based learning method. In this method, without off-line training, K-NN algorithm only needs to search through all the examples from the training data set to classify new instance. Therefore, the main calculation of K-NN is the on-line scoring of training examples to find the K Nearest Neighbors of the new instance.

Combined Group Classifiers

Recently, in the pattern recognition and machine learning domains, a combination of a number of classifiers has been known as an active research area. They can be called group or modular classifiers. The purpose of these modular classification is to obtain highly accurate results by combining weak classifier

results.[19]. Voting, Bagging and Boosting methods are a combination of techniques that we introduce here:

- **Majority voting method**

Majority voting is the simplest method to combine the classifiers. In this method, the binary output of K classifier is separately combined together. Then the class with the highest number of votes will be chosen as the final classification decision. In general, the final classification decision of the majority vote is taken from K + 1/2. Figure 7 shows the overall architecture of the modular classifier.
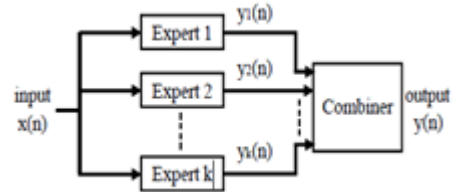

Figure 7. The overall architecture of the modular classifier. [17].

In figure 7, a number of different nervous networks (for example EXPERTS) is trained and the inputs are shared; the output of each of these is combined to create the final output.

- **Bagging method**

To improve the results of single classifier, researchers often focus on combination approaches such as Bagging. In the Bagging method, several networks are independently trained through the method of Bootstrap. [20]. Figure 8 shows the Bagging method of classification.
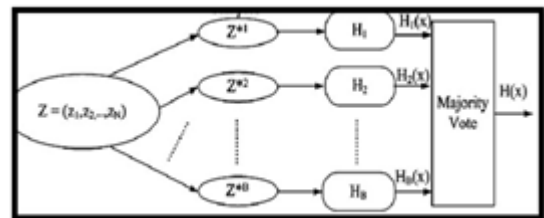

Figure 8. Classification of Bagging. [21].

In Figure 8, at first a number of training samples are generated. Each sample is given to a weaker classifier. The final classifier decision is made by the majority vote on a combination of weak classifier result output.

- **Boosting method**

Boosting is a general method for improving the performance of each learning algorithm. This approach can be used to significantly reduce errors in any "weak" learning algorithm, which constantly produces a strong classifier. Various versions of learning algorithms based on Boosting is available; Adaptive Boosting is the most popular among them (AdaBoost). For classification with two classes or two sets, 'AdaBoostM1' , 'LogitBoost' , 'GentelBoost' 'RobustBoost', 'LPBoost', 'TotalBoost', and 'Bag' can be used. For classifiers with three or more classes only 'AdaBoostM2', 'LPBoost', 'TotalBoost', 'Bag' can be used. In this paper, due to the classification of more than three classes, a copy of 'AdaBoostM2' is used. AdaBoost is a combination of Bagging and Boosting.

AdaBoost, performs the learning classifier on the weighted versions of the training set. Samples which are wrongly classified at each step will be assigned more weight in later stages. The final classifier is the linear combination of the basic classifiers. [22].

Table 1. Shows the bank creation of Gabor filter in different frequencies and directions.[15].

The number of filters	The number of direction	The number of frequency
4×7=28	7	4
3×4=12	4	3

Table 2. Shows the length of feature vector from Gabor filter feature extraction.[15].

The length of feature vector	The number of filter	The number of direction	The number of frequency
4×7×2=56	4×7=28	7	4
3×4×2=26	3×4=12	4	3

Table 3. Result of the recognition of the modality axis using Gabor filter feature in HSV color space.

feature	%Accuracy modality	Classifiers
Gabor Filter	70/80	Bayes>Naive bayes
Gabor Filter	84/90	Trees>Decision Stump
Gabor Filter	84/90	Trees>Decision Tree
Gabor Filter	84/2	Trees>j48
Gabor Filter	65/50	Trees>Random Tree
Gabor Filter	84/40	Trees>Random Forest
Gabor Filter	85/8	Bagging/WEKA
Gabor Filter	84/90	AdaBoostM2
Gabor Filter	86/4	SMO
Gabor Filter	87/20	KNN

Table 4. Result of the recognition of the direction axis using Gabor filter feature in HSV color space.

feature	%Accuracy direction	Classifiers
Gabor Filter	16/50	Bayes>Naive bayes
Gabor Filter	25/40	Trees>Decision Stump
Gabor Filter	41/80	Trees>Decision Tree
Gabor Filter	42/4	Trees>j48
Gabor Filter	25/20	Trees>Random Tree
Gabor Filter	25/20	Trees>Random Forest
Gabor Filter	50/80	Bagging/WEKA
Gabor Filter	20	AdaBoostM2
Gabor Filter	48/8	SMO
Gabor Filter	51/70	KNN

Table 5. Result of the recognition of the anatomy axis using Gabor filter feature in HSV color space.

feature	%Accuracy anatomy	Classifiers
Gabor Filter	19/80	Bayes>Naive bayes
Gabor Filter	38/90	Trees>Decision Stump
Gabor Filter	39/10	Trees>Decision Tree
Gabor Filter	44/48	Trees>j48
Gabor Filter	38/90	Trees>Random Tree
Gabor Filter	43/10	Trees>Random Forest
Gabor Filter	54/40	Bagging/WEKA
Gabor Filter	38/90	AdaBoostM2
Gabor Filter	55	SMO
Gabor Filter	55/10	KNN

Table 6. Result of the recognition of the biological system axis using Gabor filter feature in HSV color space.

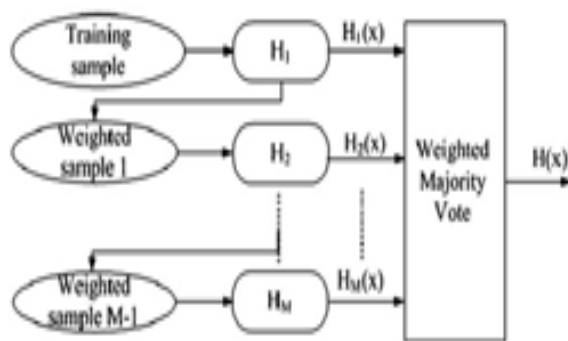| feature	%Accuracy Biological system	Classifiers
Gabor Filter	71/90	Bayes>Naive bayes
Gabor Filter	83/50	Trees>Decision Stump
Gabor Filter	83/50	Trees>Decision Tree
Gabor Filter	82/2	Trees>j48
Gabor Filter	65/40	Trees>Random Tree
Gabor Filter	75/70	Trees>Random Forest
Gabor Filter	86/1	Bagging/WEKA

Figure 9. The overall architecture of the Adaboost classifier. [21]

Random Forest

Random Forest is another combination classifier method for classification and regression which is constructed by several decisions trees during training and its output classes is obtained by individual tree outputs. This method combines Bagging with random selection of features to provide the most diverse set of decision trees. The advantage of this classifier is its very high accuracy among current algorithm classifiers and it runs effectively on large databases. This classifier handles thousands of input variables and is an efficient method to estimate data and accuracy when a large proportion of the data is missing. [9, 23].

Results and Evaluation

The overall recognition rate is a common method and is widely used for evaluation measures. It is a fraction of the test images which is predicted correctly by the 13 character IRMA code [9].

$$accuracy = \frac{correctly\ annoteted\ images}{total\ tested\ images}$$

In this method of evaluation, as a first step, one train the classifiers with training images, and after using the test images, the accuracy of the classification algorithm based on the extraction criterion is tested.

Each of the four axes of the 13 character IRMA code is reviewed, to define that for how many images of total tested images, different parts of the code have been correctly identified. For example, from among the 150 tested images in 95% of the images the first code was correctly identified, 92% of the images the second code was correctly identified; the correct identification result was 96% and 90% for the third and fourth codes respectively.

Tables3, 4, 5 and 6 show the results of the classification of (modality-direction-anatomy-biological system) using Gabor filter feature in HSV color space and distinct classifiers.

Conclusions

To annotate medical images, the aim is to produce four data axes including modality, direction, anatomy, and biological systems.

In this paper, the method of image feature extraction (Gabor Filter) is introduced, and distinct classifiers for each data axes of annotation are reviewed in order to compare the accuracy of the classifier algorithms for automatic medical image annotation. The results indicate that the K-NN classifier group provides the best results in classification (modality, direction, anatomy, and biological systems).

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