



# Comparison of Various Control Strategies for a Bioreactor Process

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## ARTICLE INFO

### Article history:

Received: 2 June 2015;

Received in revised form:  
 2 July 2015;

Accepted: 7 July 2015;

### Keywords

PID controller,  
 Adaptive control systems,  
 Adaptation gain, MIT rule,  
 Lyapunov rule,  
 Model reference adaptive control.

## ABSTRACT

Design and analysis of model reference adaptive control systems based on Massachusetts Institute of Technology (MIT) rule and Lyapunov rule are applied to a bioreactor first order process. The system is simulated using Matlab simulink and it is investigated for various values of adaptation gain of the process. Performance of the adaptive controller is compared with the PI&PID controller (using Chien–Hrones–Reswick (CHR) rule) for a step input.

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## Introduction

The use of biological processes is growing rapidly due to the increasing demand in products such as pharmaceuticals, foods, alcoholic beverages, enzymes and others. Since bioprocesses involve living organisms, they often experience nonlinear behaviours which may include output multiplicity, bifurcations, chaos, unstable dynamic response to disturbances and changes in system parameters. All these phenomena can lead to instability and ultimately affect the yield of production. Mathematical modelling and various operating conditions are discussed in [1]. Adaptive control using different rules are explained in [2]. Fed-batch bioreactor operation involving periodic addition of the substrate or nutrients is discussed [3]. An original Lyapunov based control design for the stabilization of continuous stirred tank reactor (CSTR) is proposed [4], in which a new Lyapunov function is proposed such as the control variable remains bounded. A classical absolute stability criterion is converted into nonlinear design procedures which employ efficient numerical tools, such as linear matrix inequalities (LMI). An extended circle criterion is designed which eliminates the relative degree obstacle. There restrictions on the zero dynamics are relaxed by using the Popov multiplier, which also reduces controller complexity [5]. The problem of outer-approximating the region of feasible steady states, for processes described by uncertain nonlinear differential algebraic equations including discrete variables and discrete changes in the dynamics is addressed [6]. Controller strategy is developed for a reactor which handles measured disturbances, manipulator constraints, dead time and nonlinearity [7]. Sliding-mode observers are proposed in [8], for the estimation of specific growth rate and substrate concentration from biomass measurements in fermentation processes in which global convergence is demonstrated using Lyapunov stability theory. For substrate estimation, an observer increases the convergence rate to a vicinity of the real substrate concentration to achieve asymptotic convergence despite kinetic model uncertainties are present. A process modification problem for a CSTR system [9] is worked out and solved to determine the minimal design parameter changes necessary to avoid input multiplicity. In [10],

simple control system using Proportional-Integral (PI) controllers is designed for the implementation of regulatory control structures in the operation of a Simultaneous Saccharification and Co-Fermentation (SSCF). Many methods are employed for the modelling, analysis, and control of dynamical systems based on optimization schemes, e.g., parameter estimation and model predictive control. The parameter estimation problem for a model of an isothermal continuous tube reactor is illustrated [11] and an asymptotically stable reduction error estimator is derived and analyzed for optimization. Design of MRAC using Lyapunov's theory is explained in [12] & [13]. The purpose of this paper is to design and simulate a Model Reference Adaptive control (MRAC) using two different rules for a bio reactor. Design methodology of PID controller using Chien–Hrones–Reswick (CHR) tuning Algorithm is implemented. Design of MRAC for a bioreactor process using MIT rule and Lyapunov rule is implemented and the simulation results of both the PID controller and adaptive controller methodologies are discussed followed by conclusions.

## Proposed methods

The Schematic diagram of a continuous bioreactor is shown in figure 1.

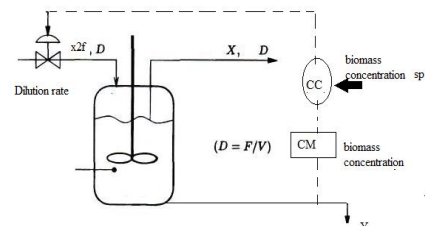


Figure 1. Schematic diagram of a continuous bioreactor

$$\frac{dx_1}{dt} = (\mu - D)x_1 \quad (1)$$

$$\frac{dx_2}{dt} = D(x_{2f} - x_2) - \frac{\mu x_1}{Y} \quad (2)$$

Where the state variables are  
 $x_1$ , the biomass concentration and  
 $x_2$ , the substrate concentration.  
 The manipulated input is  $D$ , dilution rate  
 Disturbance input is  $x_{2f}$ , substrate feed concentration  $Y$  is the  
 yield rate  
 $\mu$  is the maximum growth rate.  
 Two possible expressions for the specific growth rate are Monod  
 and substrate inhibition kinetics, which include

$$\mu = \frac{\mu_{max} x_2}{k_m + x_2} \quad \text{Monod} \quad (3)$$

$$\mu = \frac{\mu_{max} x_2}{k_m + x_2 + k_1 x_2^2} \quad \text{Substrate inhibition} \quad (4)$$

Where  
 $K_1$  is the substrate inhibition constant,  
 $K_m$  is the substrate saturation constant and  
 $\mu_{max}$  is the maximum growth rate.

#### Dynamic behaviour of a reactor

Table 1 shows the parameters to find the steady state conditions for the model shown by equations (1)&(2). The steady state dilution rate is  $D_s = 0.3 \text{ hr}^{-1}$  and the  $x_{2fs}$  is 4.0 g/ litre. Table 2 shows the operating conditions for a steady state dilution rate of  $0.3 \text{ hr}^{-1}$ . Steady state condition 1 is a washout case since no reaction was occurred. Substrate concentration is the same as feed concentration.

#### State space model of a reactor

The state space model matrices are

$$A = \begin{bmatrix} \mu_s - D_s & x_{1s} \mu_s' \\ -\frac{\mu_s}{Y} & -D_s - \frac{\mu_s' x_{1s}}{Y} \end{bmatrix}$$

$$B = \begin{bmatrix} -x_{1s} \\ x_{2fs} - x_{2s} \end{bmatrix}$$

$$\mu_s' = \frac{\partial \mu}{\partial x_{2s}} = \frac{\mu_{max} k_m}{(k_m + x_{2s})^2}$$

#### Stable operating point

The following initial condition is used for simulation

$$X(0) = \begin{bmatrix} 1.53 \\ 0.175 \end{bmatrix}$$

The state space model for the corresponding to stable operating point is

$$A = \begin{bmatrix} 0 & 0.9056 \\ -0.75 & -2.564 \end{bmatrix}$$

$$B = \begin{bmatrix} -1.5301 \\ 3.8255 \end{bmatrix}$$

$$C = [1 \quad 0]$$

$$D = [0]$$

Eigen values are determined for the above matrix and its values are  $-0.3, -2.264 \text{ hr}^{-1}$ , so the system is stable. The transfer function relating the dilution rate to the biomass concentration is determined using Matlab.

$$G_p(s) = \frac{-1.53025 - 0.4590}{s^2 + 2.5645s + 0.6792} \quad (5)$$

After pole zero cancellation the above transfer function can be written as

$$G_p(s) = \frac{-0.6758}{0.44175s + 1} e^{-0.5s} \quad (6)$$

Where the delay time is assumed as 0.5 seconds

#### Design methodology of PID controller

A typical structure of a PID control system is shown in Fig.2.

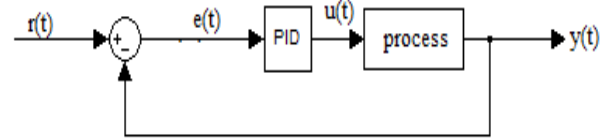


Figure 2. Structure of PID controller system

Where it can be seen that in a PID controller, the error signal  $e(t)$  is used to generate the proportional, integral, and derivative actions, with the resulting signals weighted and summed to form the control signal  $u(t)$  applied to the plant model. A mathematical description of the PID controller is

$$u(t) = K_p e(t) + \frac{1}{T_i} \int_0^t e(t) dt + T_d \frac{d}{dt} e(t) \quad (7)$$

Where  $u(t)$  is the input signal to the plant model, the error signal  $e(t)$  is defined as  $e(t) = r(t) - y(t)$ , and  $r(t)$  is the reference input signal.

#### Chien–Hrones–Reswick (CHR) PID Tuning Algorithm

The first order transfer function of a bio reactor given by equation (6) is taken for analysis which has the standard form of

$$G_p(s) = \frac{K}{sT+1} e^{-Ls} \quad (8)$$

Where  $K$  is the gain of the process and  $L$  is the delay time. The CHR PID controller tuning formulas are summarized in Table 1 for set-point regulation, in which  $a = KL/T$ ,  $T_i = L/L+T$ . Simulated results are shown in figure 1. It is observed that PID controller has less settling time and rise time compared to PI controller output. However, in both the cases % overshoot is zero.

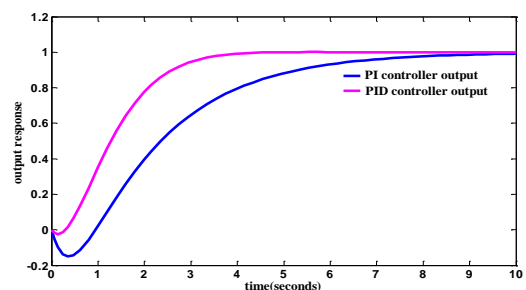


Figure 3. Comparison of PI and PID controller output response for a bioreactor process using CHR tuning algorithm

#### Model Reference Adaptive Control

This technique of adaptive control comes under the category of Non-dual adaptive control. A reference model describes system performance. The adaptive controller is then designed to force the system or plant to behave like the reference model. Model output is compared to the actual output, and the difference is used to adjust feedback controller parameters. MRAS has two loops: an inner loop or regulator loop that is an ordinary control loop consisting of the plant and regulator, and an outer or adaptation loop that adjusts the parameters of the regulator in such a way as to drive the error between the model

output and plant output to zero. MRAC scheme is shown in figure 4.

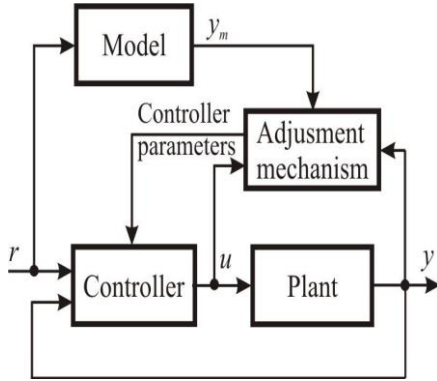


Figure 4. Parts of Model Reference Adaptive Controller

**Reference Model:** It is used to specify the ideal response of the adaptive control system to external command. It should reflect the performance specifications in control tasks. The ideal behaviour specified by the reference model should be achievable for the adaptive control system.

**Controller:** It is usually designed by a number of adjustable parameters. In this paper two parameters  $\theta_1$  and  $\theta_2$  are used to define the control law. The control law is linear in terms of the adjustable parameters (linear parameterization). Adaptive controller design normally requires linear parameterization in order to obtain adaptation mechanism with guaranteed stability and tracking convergence. The values of these control parameters are mainly dependent on adaptation gain which in turn changes the control algorithm of adaptation mechanism.

**Adaptation Mechanism:** It is used to adjust the parameters in the control law. Adaptation law searches for the parameters such that the response of the plant should be same as the reference model. It is designed to guarantee the stability of the control system as well as convergence of tracking error to zero.

Mathematical techniques like MIT rule, Lyapunov theory and theory of augmented error can be used to develop the adaptation mechanism. In this paper both MIT rule and Lyapunov rule are used for this purpose.

#### The MIT rule

This rule was developed in Massachusetts Institute of Technology and is used to apply the MRAC approach to any practical system [2]. In this rule the cost function or loss function  $J$  is defined as

$$J(\theta) = \frac{e^2}{2} \quad (9)$$

Where,  $e$  is the output error and is the difference between the output of the reference model and the actual model, while  $\theta$  is the adjustable parameter known as the control parameter.

In this rule the parameter  $\theta$  is adjusted in such a way so that the loss function is minimized. Therefore, it is reasonable to change the parameter in the direction of the negative gradient of  $J$ , with the adaptation gain  $\alpha$ , so

$$\frac{d\theta}{dt} = -\alpha e \frac{\partial e}{\partial \theta} \quad (10)$$

The partial derivative term  $\partial e / \partial \theta$ , is called the sensitivity derivative of the system. This shows how the error is dependent on the adjustable parameter,  $\theta$ . There are many alternatives to choose the loss function  $J$ . To develop the control law, equations (1), (2) are used based on MIT rule.

#### Design of MRAC using MIT rule

The plant process is given by the equation [14],

$$y_p(s) = G_p(s)U(s) = \frac{b}{s+a}U(s) \quad (11)$$

where

$$G_p(s) = \frac{b}{s+a} \quad (12)$$

is the transfer function of the process and the reference model is given by

$$y_m(s) = G_m(s)R(s) = \frac{b_m}{s+a_m}R(s) \quad (13)$$

Where  $G_m(s)$  is the T.F of the process model

The process dynamics is given by equation (14)

$$\dot{y}_p + ay_p = bu \quad (14)$$

Where  $a$  and  $b$  are known constants  $u$  is the control input. It should follow the reference dynamics

$$\dot{y}_m + a_my_m = b_mr \quad (15)$$

The control law should also includes two parameters  $\theta_1$  and  $\theta_2$ . Choosing the control law as

$$u = r\theta_1 - y_p\theta_2 \quad (16)$$

and substituting the above into equation (5) yields

$$\dot{y}_p + ay_p = b(r\theta_1 - y_p\theta_2) \quad (17)$$

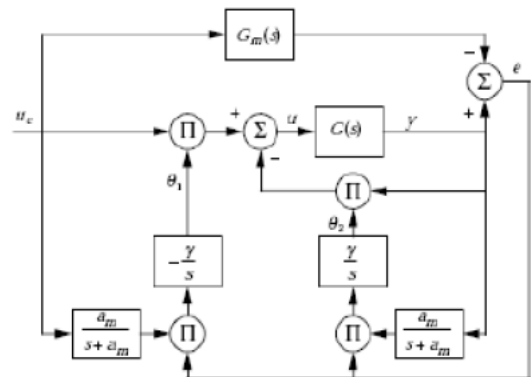
The plant dynamics should match the reference model to minimize the error, so equating (15) and (17)

$\theta_1, \theta_2$  are calculated as

$$\theta_1 = \frac{b_m}{b} \quad (18)$$

$$\theta_2 = \frac{a_m - a}{b} \quad (19)$$

The system structure using this control law is illustrated in figure 5. •



The sensitivity derivative  $\frac{d}{d\theta} e(\theta)$  is given by

$$\frac{d}{d\theta_1}(e) = \frac{d}{d\theta_1}(y_p - y_m) \quad (22)$$

Where  $e = y_p - y_m$

$$\frac{d}{d\theta_1}(e) = \frac{d}{d\theta_1} \left[ \left( \frac{b\theta_1}{s+a+b\theta_2} \right) r - y_m \right] \quad (23)$$

$$= \frac{b}{s+a+b\theta_2} r \quad (24)$$

Similarly

$$\frac{d}{d\theta_2}(e) = \frac{d}{d\theta_2}(y_p - y_m) \quad (25)$$

$$\frac{d}{d\theta_2}(e) = \frac{d}{d\theta_2} \left[ \left( \frac{b\theta_1}{s+a+b\theta_2} \right) r \right] \quad (26)$$

$$= - \left( \frac{b^2\theta_1}{(s+a+b\theta_2)^2} \right) r \quad (27)$$

$$\frac{d}{d\theta_2}(e) = \left( - \frac{b\theta_1}{s+a+b\theta_2} \right) \left( \frac{b}{s+a+b\theta_2} \right) r \quad (28)$$

$$\frac{d}{d\theta_2}(e) = - \left( \frac{b}{s+a+b\theta_2} \right) y_p \quad (29)$$

Perfect modelling is achieved by choosing

$$\theta_1 b = b_m \quad (30)$$

$a+b\theta_2 = a_m$   
Substituting equation (30) in (24) yields,

$$\frac{d}{d\theta_1}(e) = \frac{b}{s+a_m} r \quad (31)$$

$$\frac{d}{d\theta_1}(e) = \left( \frac{b}{a_m} \right) \left( \frac{a_m}{s+a_m} \right) r \quad (32)$$

Similarly, equation (29) can be written as

$$\frac{d}{d\theta_2}(e) = - \left( \frac{b}{s+a_m} \right) y_p \quad (33)$$

Substituting equations (32) and (33) in equation (10) we get,

$$\frac{d}{dt}(\theta_1) = -\alpha e \left( \frac{b}{a_m} \right) \left( \frac{a_m}{s+a_m} \right) r \quad (34)$$

$$\frac{d}{dt}(\theta_1) = -\gamma e \left( \frac{a_m}{s+a_m} \right) r \quad (35)$$

$$\frac{d}{dt}(\theta_2) = \gamma e \left( \frac{a_m}{s+a_m} \right) y_p \quad (36)$$

Where  $\gamma = \alpha \frac{b}{a_m}$  is the adaptation gain.

#### Design of MRAC Using the Lyapunov's Stability Theory

To derive an update law using Lyapunov theory, the following Lyapunov function is defined [10], [11]:

$$V = \frac{1}{2} \gamma e^2 + \frac{1}{2b} (b\theta_1 - b_m)^2 + \frac{1}{2b} (b\theta_2 + a - a_m)^2 \quad (37)$$

$$\dot{V} = \gamma e \dot{e} + \dot{\theta}_1 (b\theta_1 - b_m) + \dot{\theta}_2 (b\theta_2 + a - a_m) \quad (38)$$

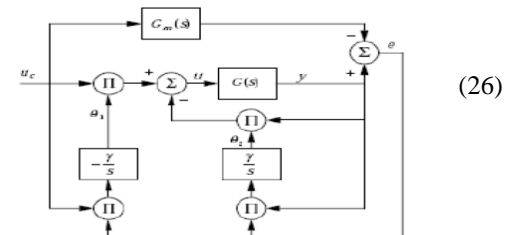
$$\dot{V} = \gamma e (\dot{y}_p - \dot{y}_m) + \dot{\theta}_1 (b\theta_1 - b_m) + \dot{\theta}_2 (b\theta_2 + a - a_m) \quad (39)$$

$$\dot{V} = -\gamma a_m e^2 + (\gamma e r + \dot{\theta}_1) (b\theta_1 - b_m) + (\dot{\theta}_2 - \gamma e y_p) (b\theta_2 + a - a_m) \quad (40)$$

$$\frac{d}{dt}(\theta_1) = -\gamma e r \quad (41)$$

$$\frac{d}{dt}(\theta_2) = \gamma e y_p \quad (42)$$

Where  $\gamma$  is the adaptation gain,  $e$  is the error,  $r$  is the reference input and  $\theta_1, \theta_2$  are the controller parameters and using the above adaptive control using Lyapunov rule is depicted in figure 6.



**Figure 6. Block Diagram Representation Of Adaptive Control Structure Based On Lyapunov Rule For A First Order Process** (26)

#### Performance evaluation of MIT rule and Lyapunov rule for a Bioreactor process

The transfer function for a bioreactor process is given by

$$G_P(S) = \frac{-0.6758}{0.44175S+1} \quad \text{and can be written as}$$

$$G_P(S) = \frac{-1.53}{S+2.264} \quad (43)$$

Which is of the form given by the equation (8), where  $a=2.264$  and  $b=1.53$

The reference model is given by

$$G_m(S) = \frac{-2}{S+2.3} \quad (44)$$

Where  $a_m=2.3$  and  $b_m=2$ . The controller parameters  $\theta_1$  and  $\theta_2$  are determined using the equations (18) and (19) respectively and are given by

$$\theta_1=1.3071$$

$$\theta_2=-0.1725.$$

The equations (34) and (35) are used in simulink diagrams represented in figure 5 and various results are shown in figures 11, 12, 13&14 using MIT rule with step input. Simulink diagram for Lyapunov rule is represented in figure 6 and corresponding results are shown in figures 7, 8, 9&10 with step input using Matlab. Figure 7 represents the comparison of model reference output and output curves for different values of  $\gamma$ . As gamma increases, the settling time decreases at the expense of overshoot and the rise time also decreases. Undershoot is 0% for all the values of  $\gamma$  for MIT rule.

Figure 8 & 9 shows the convergence of controller parameters  $\theta_1$  &  $\theta_2$  respectively. The error converges quickly to zero as  $\gamma$  value increases as shown in figure 10. Figure 11 represents the comparative analysis of model output and process output for various values of  $\gamma$  using Lyapunov's criteria. It is

observed that settling time and rise time is less compared to MIT rule. But the overshoot is highly increased as  $\gamma$  increases and undershoot also increases. Figure 12 and 13 represents the controller parameters  $\theta_1, \theta_2$  respectively, which show the sluggish response as  $\gamma$  is very small. Figure 14 represents the tracking error between the reference model and the plant which converges quickly as the adaptation gain increases. Figure 15 shows the comparative analysis of the adaptive controller using MIT rule and Lyapunov rule with the PI and PID controller outputs. Table 4 compares the results of two schemes of adaptive controller for different values of adaptation gain with PI and PID controller.

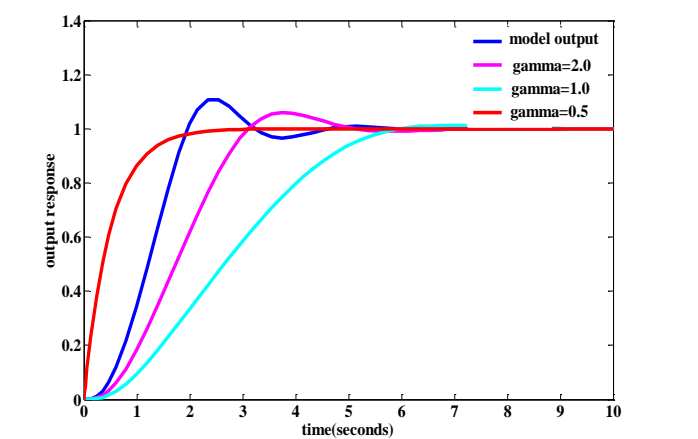


Figure 7. Comparison of Output Responses for Various Values Of  $\gamma$ ( using Lyapunov's rule)

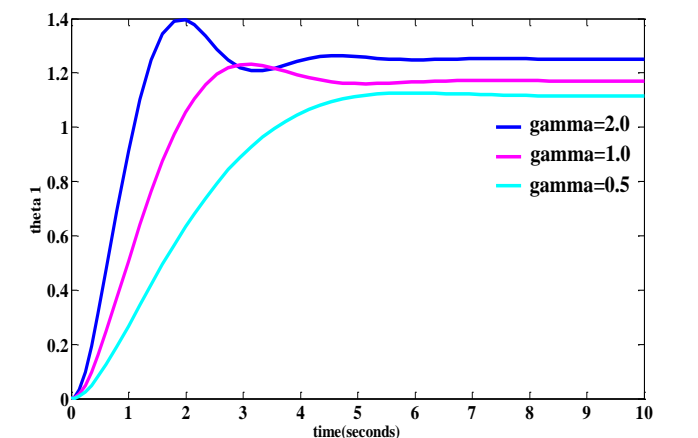


Figure 8. Variation of Controller Parameter  $\theta_1$  for Various Values Of  $\gamma$ ( using Lyapunov's rule)

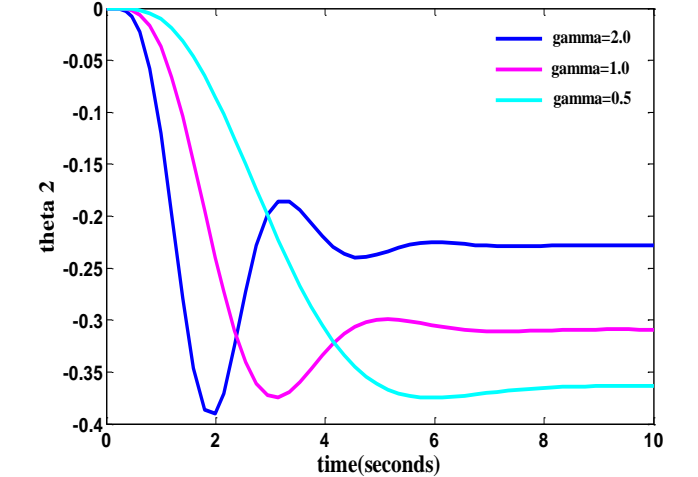


Figure 9. Variation of controller parameter  $\theta_2$  for various values of  $\gamma$  ( using Lyapunov's rule)

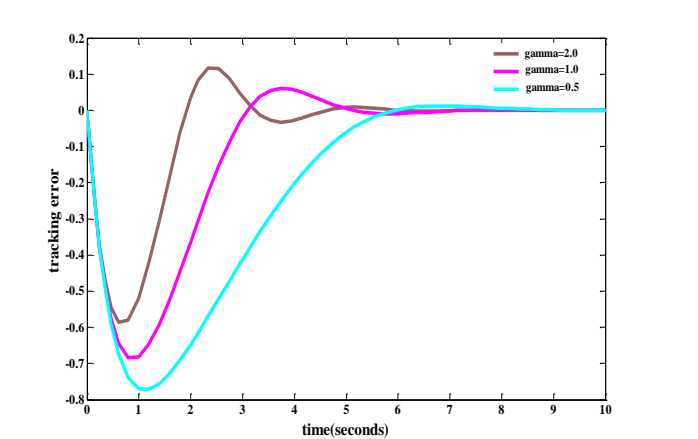


Figure 10. Tracking error for various values of  $\gamma$ ( using Lyapunov's rule)

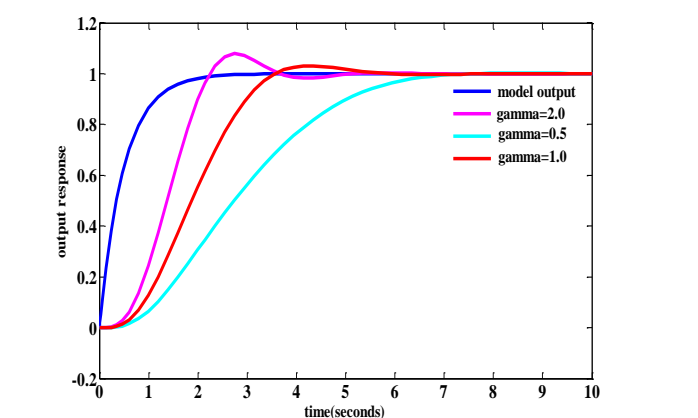


Figure 11. Comparison of output responses for various values of  $\gamma$  ( using Lyapunov's rule)

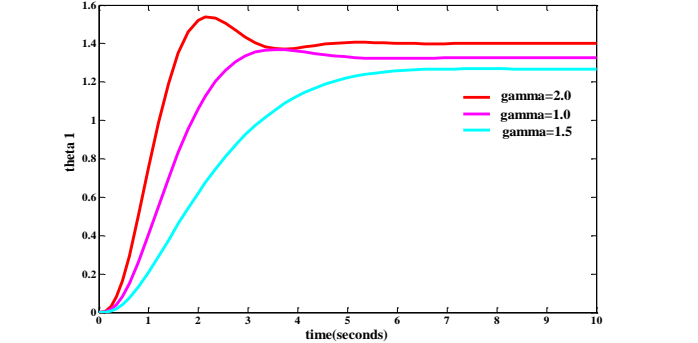


Figure 12. Variation of Controller Parameter  $\theta_1$  for Various Values Of  $\gamma$  (using MIT rule)

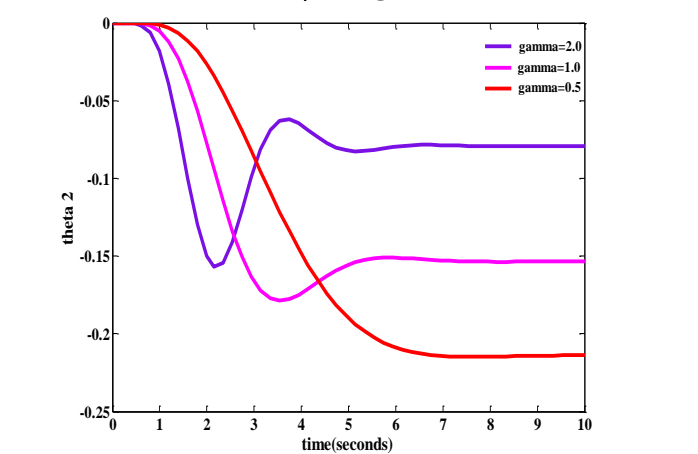


Figure 13. Variation of Controller Parameter  $\theta_2$  for various values of  $\gamma$  (using MIT rule)

Table 1. Parameters used for modelling of a bioreactor

S.No	Parameter Value
1	$\mu_{\max}=0.5\text{ hr}^{-1}$
2	$k_m=0.12\text{ g/litre}$
3	$k_1=0.4545\text{ Litre/g}$
4	$Y=0.4$

Table 2. Operating conditions of bioreactor

Sl.No	Steady State	Biomass Concentra-tion	Substrate Concentra-tion	Stability
1	Equilibrium1	$X_{1s}=0$	$X_{2s}=4.0$	stable
2	Equilibrium2	$X_{1s}=0.995$	$X_{2s}=1.5122$	unstable
3	Equilibrium3	$X_{1s}=1.53$	$X_{2s}=0.175$	stable

Table 3. CHR Tuning Formulae for Set-Point Regulation

Controller type	With 0% overshoot		
	$K_p$	$T_i$	$T_d$
PI	$0.35/a$	$1.2T$	
PID	$0.6/a$	$T$	$0.5L$

Table 4. Comparison of transient parameters for different values of  $\gamma$

Transient parameters	Model output	PID controller output		MIT rule			Lyapunov rule		
		PI controller	PID controller	$\gamma=0.5$	$\gamma=1.0$	$\gamma=2.0$	$\gamma=0.5$	$\gamma=1.0$	$\gamma=2.0$
Rise time(secs)	0.8	3.9	1.62	3.5	2.4	1.6	3.2	2	1.3
Settling time(secs)	3	7	3.46	7	6	4	6	5	4.7
%overshoot	0	0	0	0	4	6	0	5	11
%undershoot	0	0	0	0	0	0	0	1	2

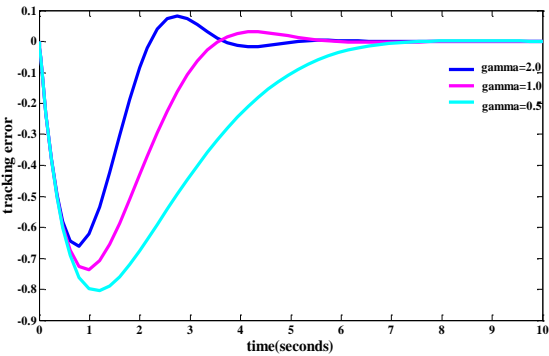


Figure 14.Tracking Error for different values of  $\gamma$  (using MIT rule)

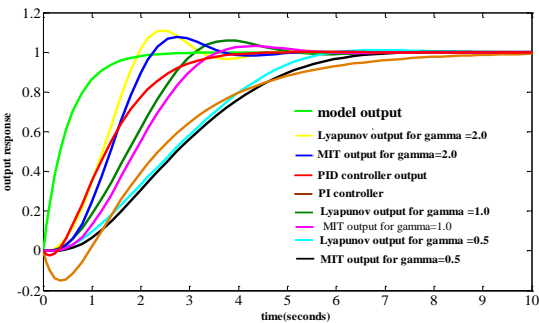


Figure 15. Comparison of Adaptive Controller (Using MIT Rule and Lyapunov Rule) With the PI and PID Controller Outputs

A detailed comparison is done between two methods of model reference adaptive control system with the conventional controller results. Simulation analysis shows that PID controller gave good response compared to adaptive controller. The range of adaptation gain is selected as 0.5, 1.0, and 2.0. It can be

observed easily that the performance of system for both the methods is improving with the increment in adaptation gain. But the rate of improvement is higher for Lyapunov theory. The system response does not have overshoot for least value of gamma, but the response is very sluggish. Now if the adaptation gain is increased slightly, response becomes oscillatory with reduction in settling time.

Conclusion

The proposed adaptive controller performance is analyzed in terms of rise time, overshoot, settling time. The conventional controller gives no overshoot. The settling time is also lesser compared to adaptive controller. Overall, the pid controller had found to be more effective and robust in response to step input compared to adaptive control strategy.

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